First look at structures

CS 6355: Structured Prediction



So far...

- Binary classifiers
 Output: 0/1
- Multiclass classifiers

 Output: one of a set of labels
- Linear classifiers for both
 Learning algorithms
- Winner-take-all prediction for multiclass

What we have seen: Training multiclass classifiers

- Label belongs to a set that has more than two elements
- Methods
 - Decomposition into a collection of binary (*local*) decisions
 - One-vs-all
 - All-vs-all
 - Error correcting codes
 - Training a single (*global*) classifier
 - Multiclass SVM
 - Constraint classification



Questions?

This lecture

• What is structured output?

• Multiclass as a structure

• Constructing outputs from pieces

Where are we?

- What is structured output?
 - Examples
- Multiclass as a structure

• Constructing outputs from pieces

Recipe for multiclass classification

- Collect a training set (hopefully with correct labels)



- Define feature representations for inputs ($x \in \Re^n$)

And, $\mathbf{y} \in \{book, dog, penguin\}$

Define linear functions to score labels

argmax $\mathbf{w}_{\mathbf{y}}^{T}\mathbf{x}$ $\mathbf{y} \in \{book, dog, penguin\}$

Natural extension to non-linear scoring functions too argmax score(x, y) $y \in \{book, dog, penguin\}$

Recipe for multiclass classification

• Train weights so that it scores examples correctly

e.g., for an input of type *book*, we want score(x, book) > score(x, penguin)
score(x, book) > score(x, dog)

- Prediction: $\underset{y \in \{book, dog, penguin\}}{\operatorname{argmax}} \operatorname{score}(x, y)$
 - Easy to predict
 - Iterate over the output list, find the highest scoring one

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What if the space of outputs is much larger? Say trees, or in general, graphs. Let's look at examples.

Example 1: Information extraction

Predicting entities and relations from text

Colin went back home to Ordon Village

Entities can be Person, Location, Organization, None

Directed edges between them can be Kill, LiveIn, WorkFor, LocatedAt, OrgBasedIn, None

Example 1: Information extraction

Predicting entities and relations from text



- Ordoi

Colin is a Person

Ordon Village is a Location

 $Colin \rightarrow OrdonVillage: \texttt{LiveIn}$

Ordon Village \rightarrow Colin None

Prediction: a structure

Structured prediction...

... requires an exploration of the combinatorial space of possible outputs to find the best one

Colin is a Location

Ordon Village is a Organization

Colin \rightarrow OrdonVillage: LiveIn

Ordon Village \rightarrow Colin LiveIn

Colin is a Person

Ordon Village is a Organization

Colin \rightarrow OrdonVillage: WorkFor

Ordon Village \rightarrow Colin LiveIn

Colin is a Person

Ordon Village is a Location

 $Colin \rightarrow OrdonVillage: \texttt{LiveIn}$

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Colin is a Organization

Ordon Village is a Person

Colin \rightarrow OrdonVillage: Kill

Ordon Village → Colin WorkFor



Example 2: Semantic Role Labeling

The task: Given a sentence, identify who does what to whom, where and when.

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The bus was *heading* for Nairobi in Kenya

Relation: to head Mover[A0]: the bus Destination[A1]: Nairobi in Kenya

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The task: Given a sentence, identify who does what to whom, where and when.



- 1. Identify candidate arguments for verb using parse tree
 - Filtered using a binary classifier

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 - Multi-class classifier (one of multiple labels per candidate)



Each color is a different label here

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3. Inference

- Using probability estimates from argument classifier
- Must respect structural and linguistic constraints
 - Eg: The same word can not be part of two arguments



The bus was **heading** for Nairobi in Kenya.



Suppose we are assigning colors to each span

Special label, meaning "Not an argument"















Structured output is...

- A data structure with a pre-defined schema
 - Eg: SRL converts raw text into a record in a database

Predicate	AO	A1	Location
Head	The bus	Nairobi in Kenya	-

- Equivalently, a *graph*
 - Often restricted to be a specific family of graphs: chains, trees, etc



Questions/comments?

Example 3: Object detection



Example 3: Object detection



Example 3: Object detection



The output: A schematic showing the parts and their relative layout



Once again, a structure



Left wheel detector: Is there a wheel in this box? Binary classifier



Handle bar detector: Is there a handle bar in this box? Binary classifier



1. Left wheel detector

2. Right wheel detector

3. Handle bar detector

4. Seat detector



1. Left wheel detector

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Final output: Combine the predictions of these individual classifiers (local classifiers)

The predictions interact with each other

Eg: The same box can not be both a left wheel and a right wheel, handle bar does not overlap with seat,...

Need inference to *construct* the output

Example 4: Sequence labeling

More on this in next lecture

- Input: A sequence of *tokens* (like words)
- Output: A sequence of labels of same length as input
- Eg: Part-of-speech tagging:

Given a sentence, find parts-of-speech of all the words
Example 4: Sequence labeling

More on this in next lecture

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Determiner	Noun	Verb	Noun	Noun

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The	Fed	raises	interest	rates
Determiner	Noun	Verb	Noun	Noun
Other labels are possible in different contexts	Verb (I <u>fed</u> thedog)	(Poems	Verb don't <u>interest</u> me)	Verb (He <u>rates</u> movies online)

Given a word, its label depends on :

The identity and characteristics of the word

E.g. Raises is a Verb because it ends in -es (among other reasons)

- Its grammatical context
 - Fed in "The Fed" is a Noun because it follows a Determiner
 - Fed in "I fed the.." is a Verb because it follows a Pronoun

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One possible modeling assumption:

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Two kinds of scoring functions for labels

- 1. Score for label associating with a particular word in context
- 2. Score for a pair of labels following each other

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Two kinds of scoring functions for labels

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What we want: Find a sequence of labels that *maximizes* the sum/product of these scores

More examples

Protein 3D structure prediction

AMADLEQKVLEMEASTYDGVFIWKISDFARKRQEAVAGRIPAIFSPAFYTHHHHHHHHHHHHHSSSEEEEEEESHHHHHHHHHTTSSEEEEEESRYGYKMCLRIYLNGDGTGRGTHLSLFFVVMKGPNDALLRWPFNQKVTLMSTTSEEEEEETGGGTTTEEEEEEEEETTGGGSSSEEEELLDQNNREHVIDAFRPDVTSSSFQRPVNDMNIASGCPLFCPVSKMEAKNSETTSSEEEEETTSGGGSSSSBEEEEEEEETTTTTTSTTYVRDDAIFIKAIVDLTGLTSSEEEEEEEETTSSEEEEESSSS



Inferring layout of a room



Image from [Schwing et al 2013]

Structured output is...

- A graph, possibly labeled and/or directed
 - Possibly from a restricted family, such as chains, trees, etc.
 - A discrete representation of input
 - Eg. A table, the SRL frame output, a sequence of labels etc
- A collection of inter-dependent decisions
 - Eg: The sequence of decisions used to construct the output
- The result of a combinatorial optimization problem $\underset{y \in \textit{ all outputs}}{\operatorname{argmax}} score(\mathbf{x}, \mathbf{y})$

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Representation

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There are a countable number of graphs Question: Why can't we treat each output as a label and train/predict as multiclass? We have seen something similar before in the context of multiclass

Challenges with structured output

Two challenges

- 1. We cannot train a separate weight vector for each possible inference outcome
 - For multiclass, we could train one weight vector for each label
- 2. We cannot enumerate all possible structures for inference
 - Inference for multiclass was easy

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Solution

- Decompose the output into parts that are labeled
- Define
 - how the parts interact with each other
 - how these labeled interacting parts are scored
 - an inference algorithm to assign labels to all the parts so that the whole is meaningful

Where are we?

• What is structured output?

- Multiclass as a structure
 - A very brief digression
- Constructing outputs from pieces

Multiclass as a structured output

- A structure is...
 - A graph (in general, hypergraph), possibly labeled and/or directed
 - A collection of interdependent decisions

The output of a combinatorial optimization problem
argmax score(x, y)
y∈ all outputs

- Multiclass
 - A graph with one node and no edges
 - Node label is the output
 - Can be composed via multiple decisions

- Winner-take-all argmax $\mathbf{w}^{T} \phi(\mathbf{x}, i)$

Multiclass is a structure: Implications

- 1. A lot of the ideas from multiclass <u>may</u> be generalized to structures
 - Not always simple, but useful to keep in mind
- 2. Broad statements about structured learning must apply to multiclass classification
 - Useful for sanity check, also for understanding
- 3. Binary classification is the most "trivial" form of structured classification
 - Multiclass with two classes

Where are we?

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Decomposing the output

- We need to produce a graph
 - We cannot enumerate all possible graphs for the argmax
- Solution: Think of the graph as combination of many smaller parts
 - The parts should agree with each other in the final output
 - Each part has a score
 - The total score for the graph is the sum of scores of each part
- Decomposition of the output into parts also helps generalization
 - Why?



Setting

Output: Nodes and edges are labeled and the blue and orange edges form a tree



The scoring function scores outputs

For generalization and ease of inference, break the output into parts and score each part The score for the structure is the sum of the part scores

What is the best way to do this decomposition? Depends....

3 possible edge labels



Setting

Output: Nodes and edges are labeled and the blue and orange edges form a tree



3 possible edge labels

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Goal: Find the highest scoring labeling such that the edges that are colored form a tree

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Note: The output **y** is a labeled assignment of the nodes and edges



The input **x** not shown here



One option: Decompose fully. All nodes and edges are independently scored



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s.t.

y forms a tree

Setting

Output: Nodes and edges are labeled and the blue and orange edges form a tree



One option: Decompose fully. All nodes and edges are independently scored



У

Still need to ensure that the colored edges form a valid output (i.e. a tree)

This is invalid output! Even this simple decomposition requires *inference* to ensure validity

Setting

Output: Nodes and edges are labeled and the blue and orange edges form a tree

Goal: Find the highest scoring labeling such that the edges that are colored form a tree

 $\operatorname{score}(\mathbf{x}, \mathbf{y}) = \sum_{n \in \operatorname{nodes}(\mathbf{x}, \mathbf{y})} \operatorname{score}(n) + \sum_{e \in \operatorname{edges}(\mathbf{x}, \mathbf{y})} \operatorname{score}(e)$ Prediction: $\operatorname{arg\,max} \operatorname{score}(\mathbf{x}, \mathbf{y})$

s.t. **y** forms a tree

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Another possibility: Score each edge and its nodes together



Setting

Output: Nodes and edges are labeled and the blue and orange edges form a tree



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 $e \in edges(\mathbf{x}, \mathbf{y})$



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Inference should ensure that

- 1. The output is a tree, and
- 2. Shared nodes have the same label in all the pieces



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We have seen two examples of decomposition

Many other decompositions possible...

Inference

- Each part is scored independently
 - Key observation: Number of possible inference outcomes for each part may not be large
 - Even if the number of possible structures might be large
- Inference: How to glue together the pieces to build a valid output?
 - Depends on the "shape" of the output
- Computational complexity of inference is important
 - Worst case: intractable
 - With assumptions about the output, polynomial algorithms exist.
 - We may encounter some examples in more detail:
 - Predicting sequence chains: Viterbi algorithm
 - To parse a sentence into a tree: CKY algorithm
 - In general, might have to either live with intractability or approximate

Questions?

Training regimes

- Decomposition of outputs gives two approaches for training
 - Decomposed training/Learning without inference
 - Learning algorithm does not use the prediction procedure during training
 - Global training/Joint training/Inference-based training
 - Learning algorithm uses the final prediction procedure during training
- Similar to the two strategies we had before with multiclass
- Inference complexity often an important consideration in choice of modeling and training
 - Especially so if full inference plays a part during training
 - Ease of training smaller/less complex models could give intermediate training strategies between fully decomposed and fully joint

Computational issues

Background **knowledge** about domain

Computational issues










Summary

- We saw several examples of structured output
 - Structures are graphs
 - Sometimes useful to think of them as a sequence of decisions
 - Also useful to think of them as data structures
- Multiclass is the simplest type of structure
 - Lessons from multiclass are useful
- Modeling outputs as structures
 - Decomposition of the output, inference, training

Questions?

Next steps...

- Sequence prediction
 - Markov model
 - Predicting a sequence
 - Viterbi algorithm
 - Training
 - MEMM, CRF, structured perceptron for sequences
- After sequences
 - General representation of probabilistic models
 - Bayes Nets and Markov Random Fields
 - Generalization of global training algorithms to arbitrary conditional models
 - Inference techniques
 - More on Conditional models, constraints on inference