Machine Learning



#### Outline

The Perceptron Algorithm

Variants of Perceptron

Perceptron Mistake Bound

#### Where are we?

The Perceptron Algorithm

Variants of Perceptron

Perceptron Mistake Bound

#### Recall: Linear Classifiers

Inputs are d dimensional vectors, denoted by  $\mathbf{x}$  Output is a label  $y \in \{-1, 1\}$ 

Linear Threshold Units classify an example  $\mathbf{x}$  using parameters  $\mathbf{w}$  (a d dimensional vector) and  $\mathbf{b}$  (a real number) according the following classification rule

Output = 
$$sign(\mathbf{w}^T\mathbf{x} + b) = sign(\sum_i w_i x_i + b)$$
  

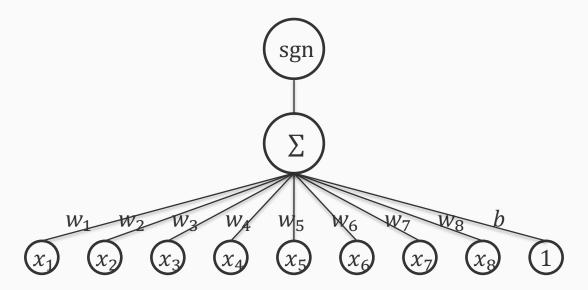
$$\mathbf{w}^T\mathbf{x} + b \ge 0 \Rightarrow y = +1$$
  

$$\mathbf{w}^T\mathbf{x} + b < 0 \Rightarrow y = -1$$

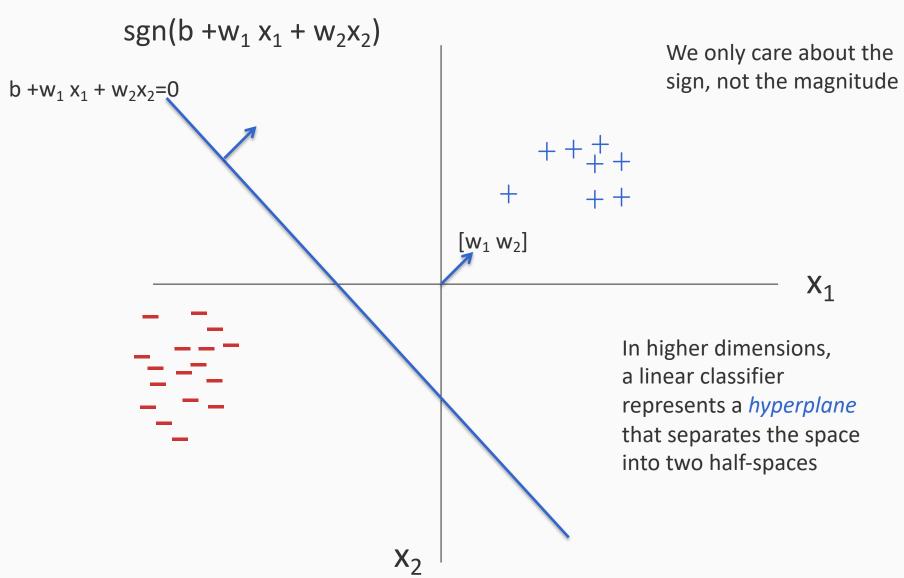
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# The geometry of a linear classifier



#### The Perceptron

REPORT NO. 85-460-1

THE PERCEPTRON

A PERCEIVING AND RECOGNIZING AUTOMATON

(PROJECT PARA)

January, 1957

Prepared by: Frank Rosenblat

Frank Rosenblatt, Project Engineer

Psychological Review Vol. 65, No. 6, 1958

# THE PERCEPTRON: A PROBABILISTIC MODEL FOR INFORMATION STORAGE AND ORGANIZATION IN THE BRAIN <sup>1</sup>

F. ROSENBLATT

Cornell Aeronautical Laboratory

- Introduced by Rosenblatt (1958)
  - Though there were some hints of a similar idea earlier Agmon (1954), Motzkin and Schonberg (1954)
- The goal is to find a separating hyperplane
   For separable data, guaranteed to find one
- An online algorithm
   That is, it processes one example at a time
- A mistake-driven algorithm
   That is, it makes updates if, and only if, it makes a mistake on an example
- Several variants exist
   We will see these briefly at towards the end

Input: A sequence of training examples  $(\mathbf{x}_1, y_1), (\mathbf{x}_2, y_2), \cdots$ where all  $\mathbf{x}_i \in \mathbb{R}^d, y_i \in \{-1, 1\}$ 

Input: A sequence of training examples  $(\mathbf{x}_1, y_1), (\mathbf{x}_2, y_2), \cdots$ where all  $\mathbf{x}_i \in \mathbb{R}^d, y_i \in \{-1, 1\}$ 

1. Initialize  $\mathbf{w}_0 = 0 \in \mathbb{R}^d$ 

3. Return final weight vector

Input: A sequence of training examples  $(\mathbf{x}_1, y_1), (\mathbf{x}_2, y_2), \cdots$ where all  $\mathbf{x}_i \in \mathbb{R}^d, y_i \in \{-1, 1\}$ 

- 1. Initialize  $\mathbf{w}_0 = 0 \in \mathbb{R}^d$
- 2. For each training example  $(\mathbf{x}_i, y_i)$ :
  - 1. Predict  $y' = sgn(\mathbf{w}_t^T \mathbf{x}_i)$

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    - Update  $\mathbf{w}_{t+1} \leftarrow \mathbf{w}_t + r(y_i \mathbf{x}_i)$
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#### Remember:

Prediction =  $sgn(\mathbf{w}^T\mathbf{x})$ 

There is typically a bias term also  $(\mathbf{w}^T\mathbf{x} + \mathbf{b})$ , but the bias may be treated as a constant feature and folded into  $\mathbf{w}$ 

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Mistake on positive:  $\mathbf{w}_{t+1} \leftarrow \mathbf{w}_t + r\mathbf{x}_i$ Mistake on negative:  $\mathbf{w}_{t+1} \leftarrow \mathbf{w}_t - r\mathbf{x}_i$ 

- 1. Initialize  $\mathbf{w}_0 = 0 \in \Re^d$
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r is the learning rate, a small positive number less than 1

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Update only on error. A mistake-driven algorithm

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Update only on error. A mistake-driven algorithm

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This is the simplest version. We will see more robust versions shortly

```
Mistake on positive: \mathbf{w}_{t+1} \leftarrow \mathbf{w}_t + r\mathbf{x}_i
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```

Suppose we have made a mistake on a positive example That is, y = +1 and  $\mathbf{w}_t^T \mathbf{x} \leq 0$ 

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Call the new weight vector  $\mathbf{w}_{t+1} = \mathbf{w}_t + \mathbf{x}$  (say r = 1)

Mistake on positive:  $\mathbf{w}_{t+1} \leftarrow \mathbf{w}_t + r\mathbf{x}_i$ Mistake on negative:  $\mathbf{w}_{t+1} \leftarrow \mathbf{w}_t - r\mathbf{x}_i$ 

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That is, y = +1 and  $\mathbf{w}_t^{\mathrm{T}} \mathbf{x} \leq 0$ 

Call the new weight vector  $\mathbf{w}_{t+1} = \mathbf{w}_t + \mathbf{x}$  (say r = 1)

The new dot product is  $\mathbf{w}_{t+1}^T\mathbf{x} = (\mathbf{w}_t + \mathbf{x})^T\mathbf{x} = \mathbf{w}_t^T\mathbf{x} + \mathbf{x}^T\mathbf{x} \geq \mathbf{w}_t^T\mathbf{x}$ 

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For a positive example, the Perceptron update will increase the score assigned to the same input

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 and  $\mathbf{w}_t^{\mathrm{T}} \mathbf{x} \leq 0$ 

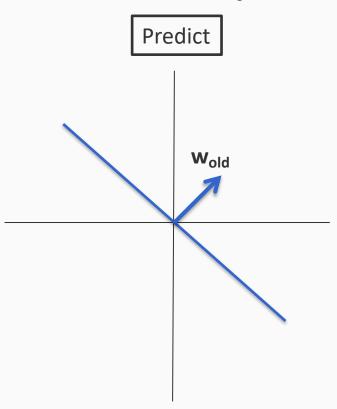
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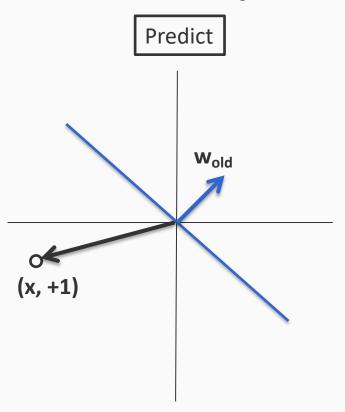
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Similar reasoning for negative examples

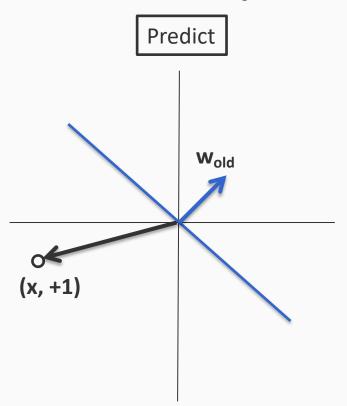
# Geometry of the perceptron update



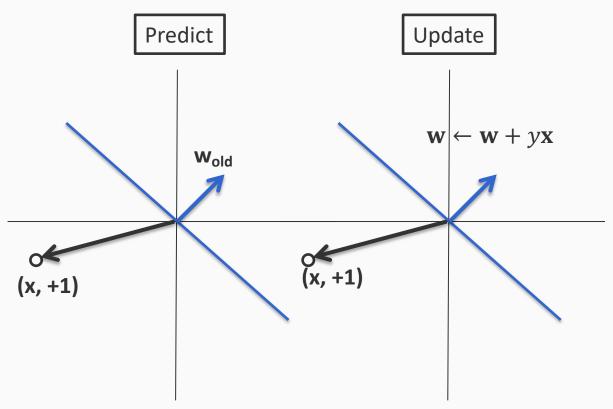
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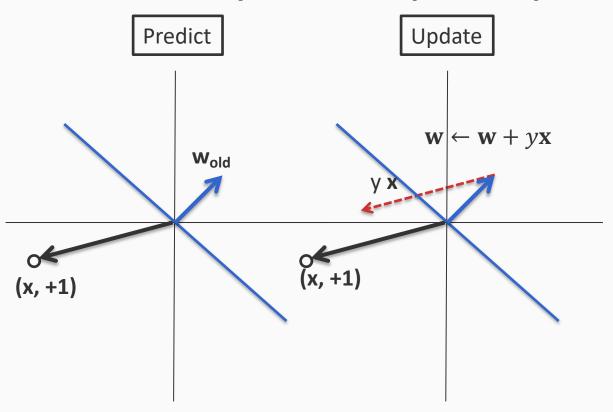
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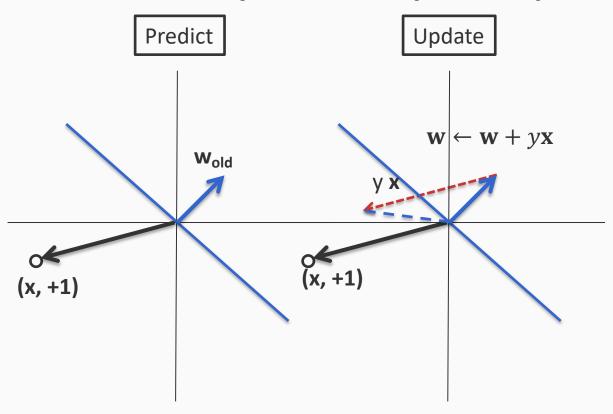
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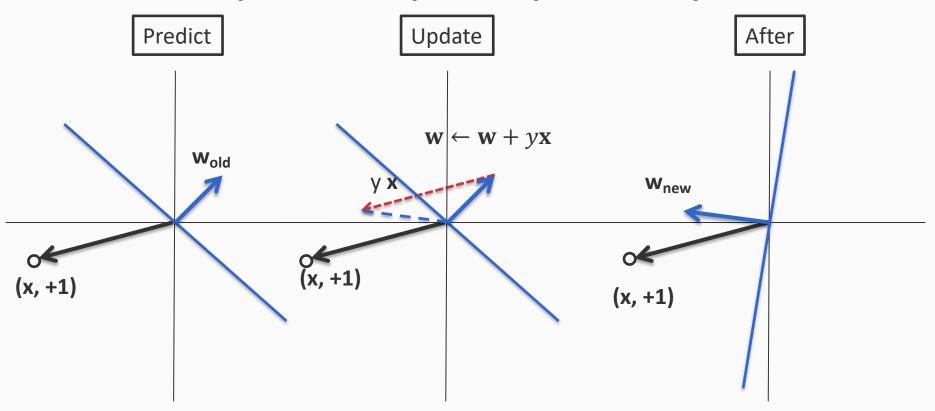
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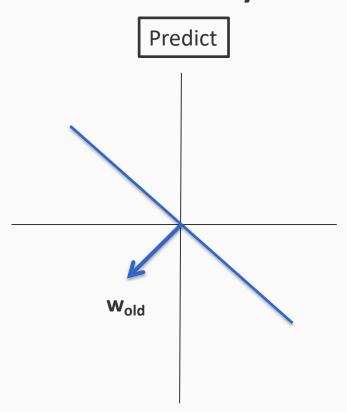
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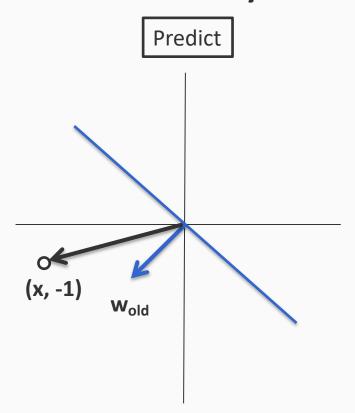


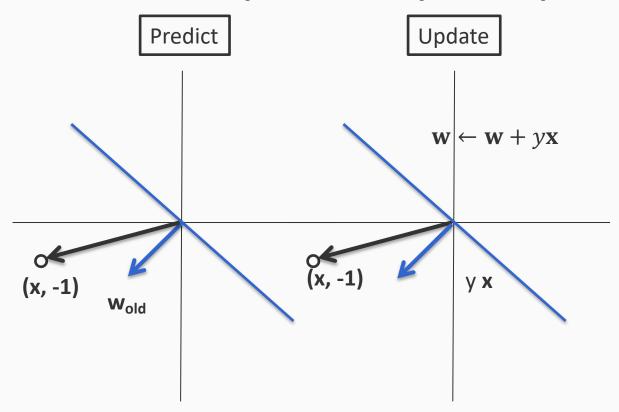
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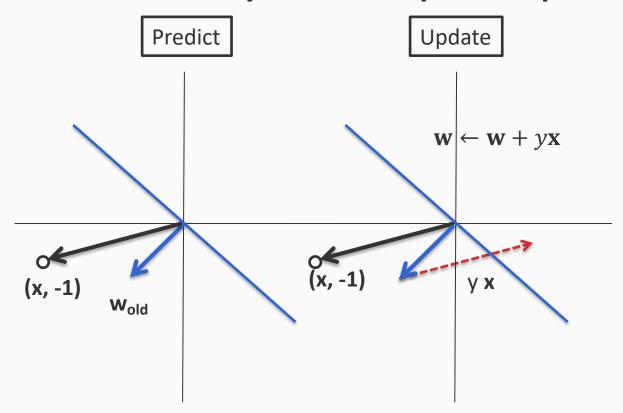


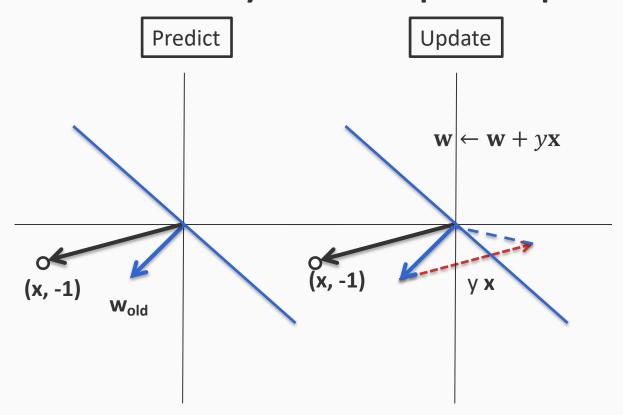
For a mistake on a positive example



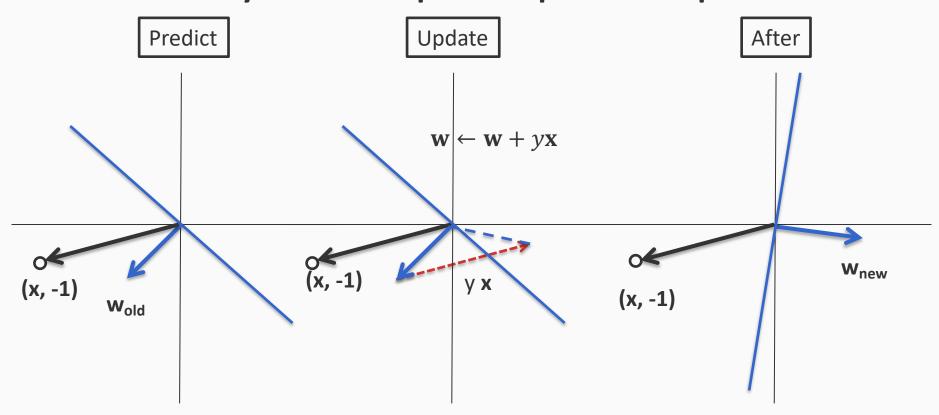








### Geometry of the perceptron update



For a mistake on a negative example

#### Where are we?

The Perceptron Algorithm

Variants of Perceptron

Perceptron Mistake Bound

#### Practical use of the Perceptron algorithm

1. Using the Perceptron algorithm with a finite dataset

2. Voting and Averaging

3. Margin Perceptron

# 1. The "standard" algorithm

Given a training set  $D = \{(\mathbf{x}_i, y_i)\}$  where  $\mathbf{x}_i \in \mathbb{R}^d$ ,  $y_i \in \{-1, 1\}$ 

- 1. Initialize  $\mathbf{w} = \mathbf{0} \in \mathbb{R}^d$
- 2. For epoch in  $1 \cdots T$ :
  - 1. Shuffle the data
  - 2. For each training example  $(\mathbf{x}_i, y_i) \in D$ :
    - If  $y_i \mathbf{w}^T \mathbf{x}_i \leq 0$ , then:
      - update  $\mathbf{w} \leftarrow \mathbf{w} + ry_i \mathbf{x}_i$
- 3. Return w

Prediction on a new example with features  $\mathbf{x}$ :  $\operatorname{sgn}(\mathbf{w}^T\mathbf{x})$ 

## 1. The "standard" algorithm

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- 2. For epoch in  $1 \cdots T$ :

T is a hyper-parameter to the algorithm

- 1. Shuffle the data
- 2. For each training example  $(\mathbf{x}_i, y_i) \in D$ :
  - If  $y_i \mathbf{w}^T \mathbf{x}_i \leq 0$ , then:

Another way of writing that there is an error

- update  $\mathbf{w} \leftarrow \mathbf{w} + ry_i \mathbf{x}_i$ 

3. Return w

Prediction on a new example with features  $\mathbf{x}$ :  $\operatorname{sgn}(\mathbf{w}^T\mathbf{x})$ 

### 2. Voting and Averaging

- So far: We return the final weight vector
- Voted perceptron
  - Remember every weight vector in your sequence of updates.
  - At final prediction time, each weight vector gets to vote on the label. The number of votes it gets is the number of iterations it survived before being updated
  - Comes with strong theoretical guarantees about generalization, impractical because of storage issues

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So far: We return the final weight vector

#### Voted perceptron

- Remember every weight vector in your sequence of updates.
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- Comes with strong theoretical guarantees about generalization, impractical because of storage issues

#### Averaged perceptron

- Instead of using all weight vectors, use the average weight vector (i.e. longer surviving weight vectors get more say)
- More practical alternative and widely used

### Averaged Perceptron

Given a training set  $D = \{(\mathbf{x}_i, y_i)\}$  where  $\mathbf{x}_i \in \mathbb{R}^d$ ,  $y_i \in \{-1, 1\}$ 

- 1. Initialize  $\mathbf{w} = \mathbf{0} \in \mathbb{R}^d$  and  $\mathbf{a} = \mathbf{0} \in \mathbb{R}^d$
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  - 2. For each training example  $(\mathbf{x}_i, y_i) \in D$ :
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      - update  $\mathbf{w} \leftarrow \mathbf{w} + ry_i \mathbf{x}_i$
    - $a \leftarrow a + w$
- 3. Return a

Prediction on a new example with features  $\mathbf{x}$ :  $sgn(\mathbf{a}^T\mathbf{x})$ 

#### Averaged Perceptron

Given a training set  $D = \{(\mathbf{x}_i, y_i)\}$  where  $\mathbf{x}_i \in \mathbb{R}^d$ ,  $y_i \in \{-1, 1\}$ 

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This is the simplest version of the averaged perceptron

There are some easy programming tricks to make sure that **a** is also updated only when there is an error

Prediction on a new example with features  $\mathbf{x}$ :  $\operatorname{sgn}(\mathbf{a}^T\mathbf{x})$ 

#### **Averaged Perceptron**

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- 3. Return a

This is the simplest version of the averaged perceptron

There are some easy programming tricks to make sure that **a** is also updated only when there is an error

If you want to use the Perceptron algorithm, use averaging

Prediction on a new example with features  $\mathbf{x}$ :  $\operatorname{sgn}(\mathbf{a}^T\mathbf{x})$ 

### 3. Margin Perceptron

Perceptron makes updates only when the prediction is incorrect

$$y_i \mathbf{w}^T \mathbf{x}_i \leq 0$$

• What if the prediction is close to being incorrect? That is, Pick a small positive  $\eta$  and update when

$$y_i \mathbf{w}^T \mathbf{x}_i \leq \eta$$

• Can generalize better, but extra hyper-parameter  $\eta$  Exercise: Why is the margin perceptron a good idea?

#### The Perceptron

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# THE PERCEPTRON: A PROBABILISTIC MODEL FOR INFORMATION STORAGE AND ORGANIZATION IN THE BRAIN <sup>1</sup>

F. ROSENBLATT

Cornell Aeronautical Laboratory

# The hype

#### NEW NAVY DEVICE LEARNS BY DOING

Psychologist Shows Embryo of Computer Designed to Read and Grow Wiser

WASHINGTON, July 7 (UPI)
—The Navy revealed the embryo of an electronic computer
today that it expects will be
able to walk, talk, see, write,
reproduce itself and be conscious of its existence.

The embryo—the Weather Bureau's \$2,000,000 "704" computer—learned to differentiate between right and left after fifty attempts in the Navy's demonstration for newsmen.

The service said it would use this principle to build the first of its Perceptron thinking machines that will be able to read and write. It is expected to be finished in about a year at a cost of \$100,000. HAVING told you about the giant digital computer known as I.B.M. 704 and how it has been taught to play a fairly creditable game of chess, we'd like to tell you about an even more remarkable machine, the perceptron, which, as its name implies, is capable of what amounts to original thought. The first perceptron has yet to be built,

The New Yorker, December 6, 1958 P. 44

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The IBM 704 computer

## What you need to know

The Perceptron algorithm

The geometry of the update

What can it represent

Variants of the Perceptron algorithm