

Attention in NLP



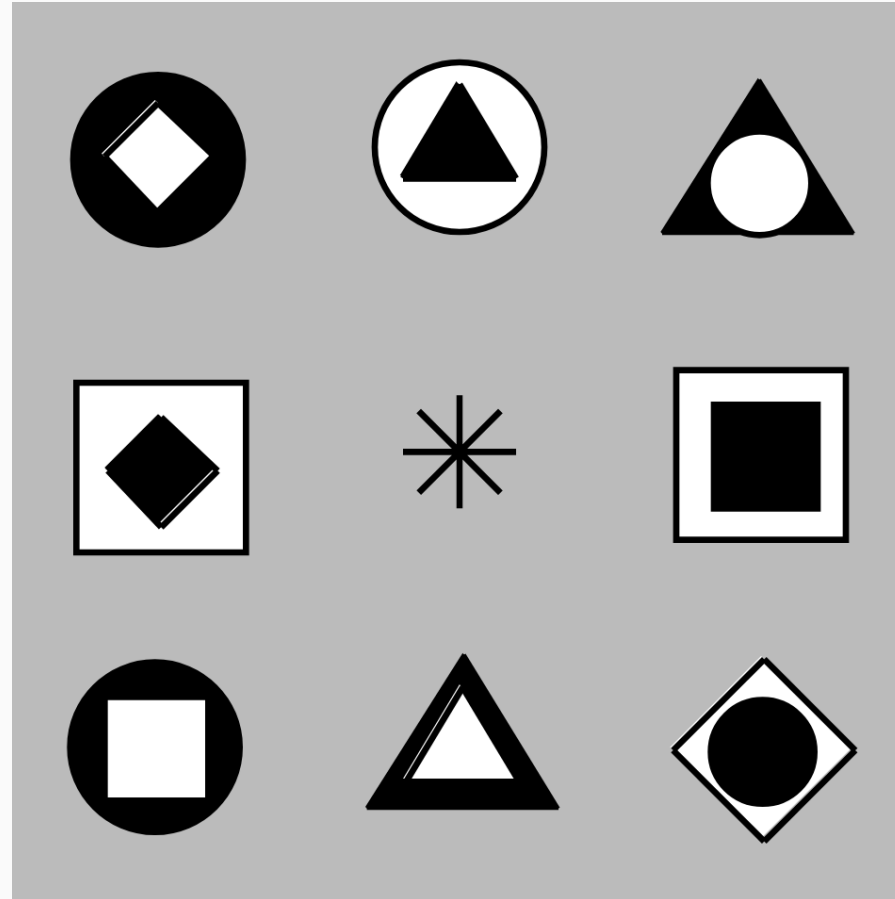
Overview

- What is attention?
- Attention in encoder-decoder networks
- Various kinds of attention

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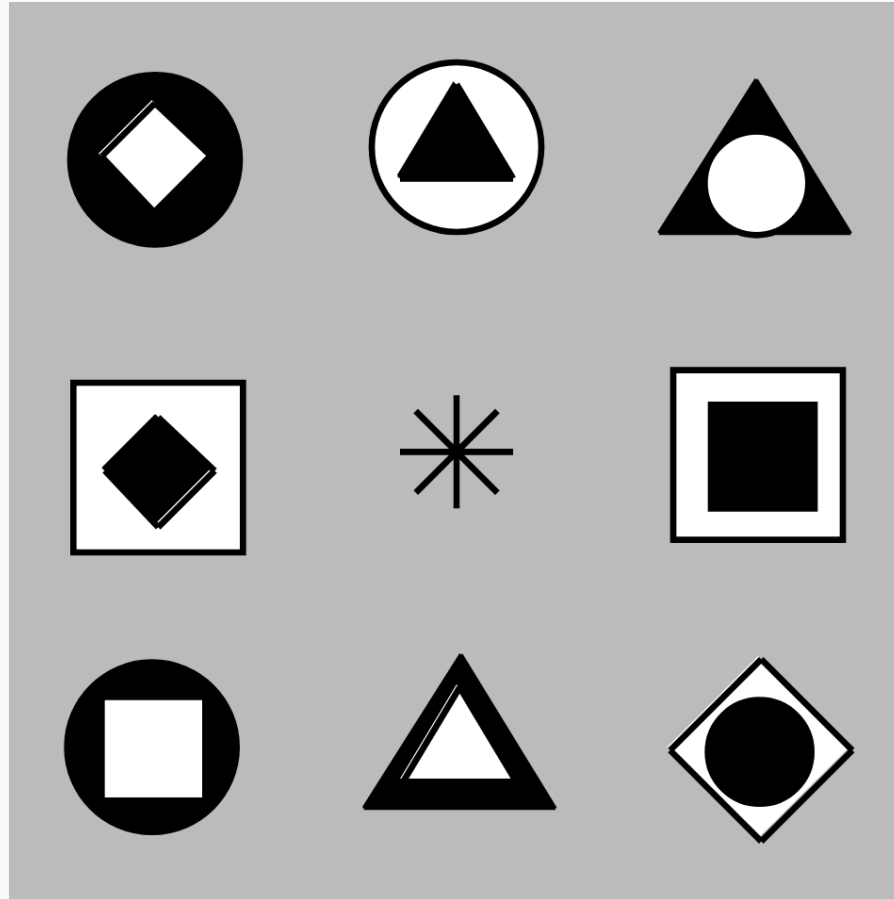
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Visual attention



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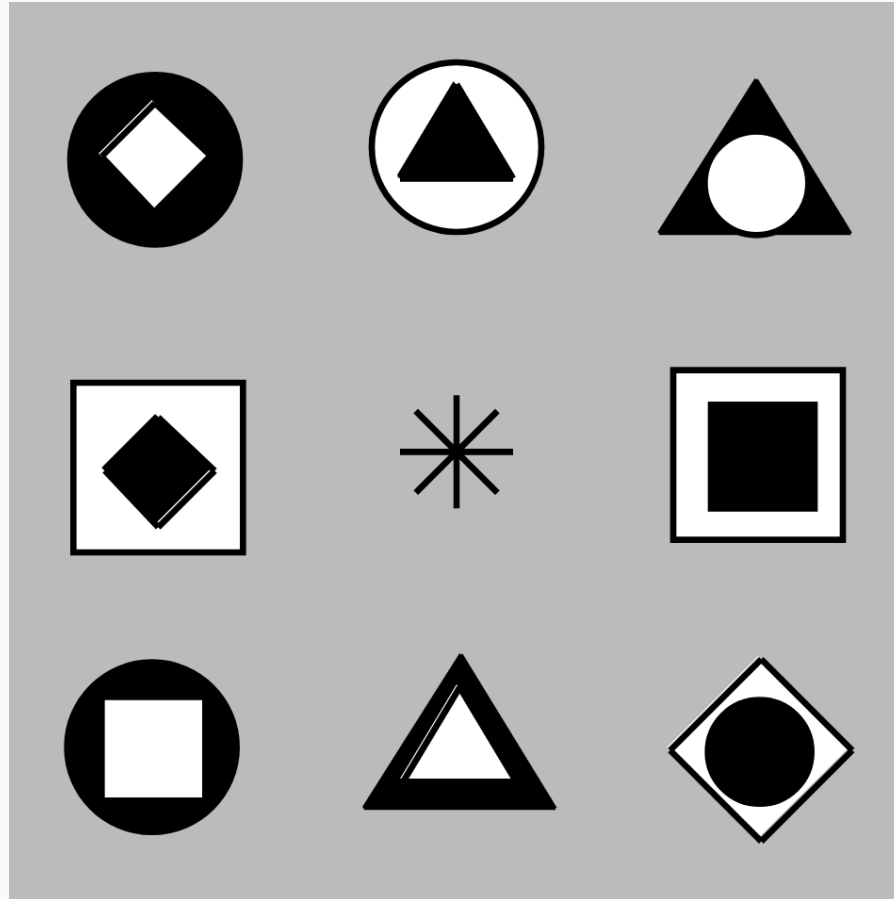
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Now (without changing focus) where is the black circle containing a white square?

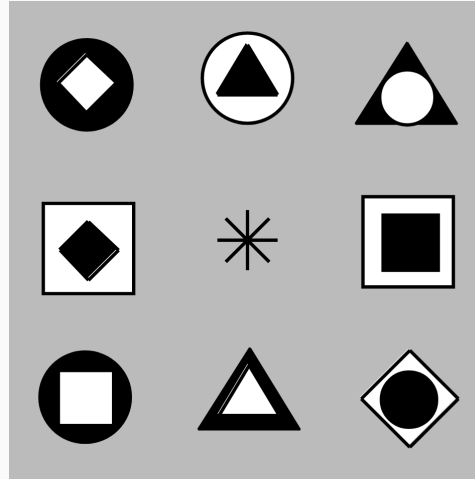
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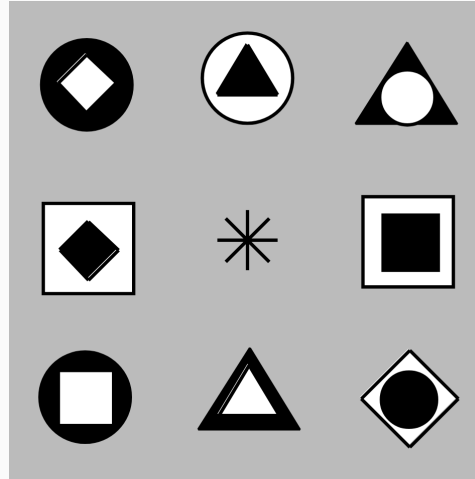
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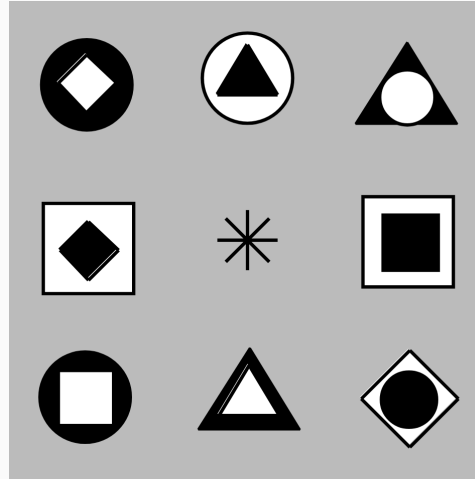
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In other words, you exercised your *visual attention*

What is attention?

- All inputs may not need careful processing at all points of time
- Attention: A mechanism for selecting a subset of information for further analysis, processing, or computation
 - *Focus* on the most relevant information, and ignore the rest
- Widely studied in cognitive psychology, neuroscience and related fields
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What to focus on is also a decision problem

Who makes that decision?

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- First introduced in the context of encoder-decoder networks for machine translation
- Generally it takes the following form:
 - We have a large input, but need to focus on only a small part
 - An auxiliary network predicts a distribution over the input that decides the attention over its parts
 - The output is the weighted sum of the attention and the input

Example application: Machine Translation

Suppose we have to convert a Dutch sentence into its English translation

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This requires us to consume a sequence and generate a new one that means the same

Consuming and generating sequences

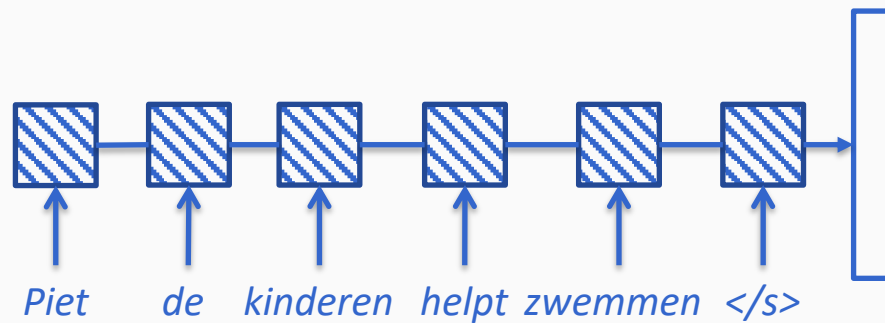
Recurrent neural networks as general sequence processors

- RNNs can encode a sequence into sequence of state vectors
- RNNs can generate sequences starting with an initial input
 - And can even take inputs at each step to guide the generation

The encoder-decoder approach

[Sutskever, et al 2014, Cho et al 2014]

Encode the input using an RNN till a special end-of-input token is reached
(Could be a bi-directional RNN)



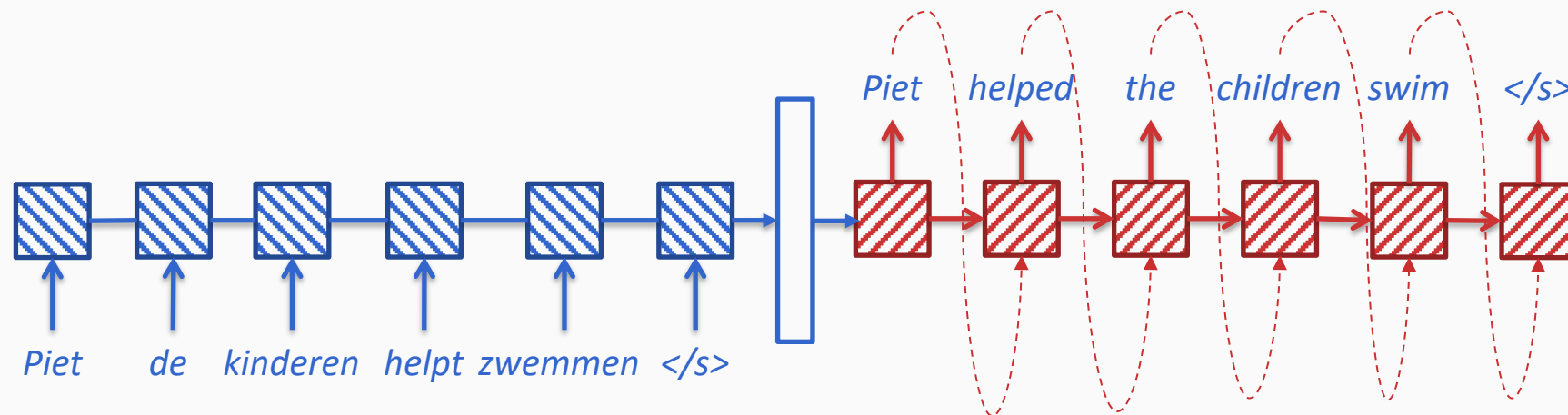
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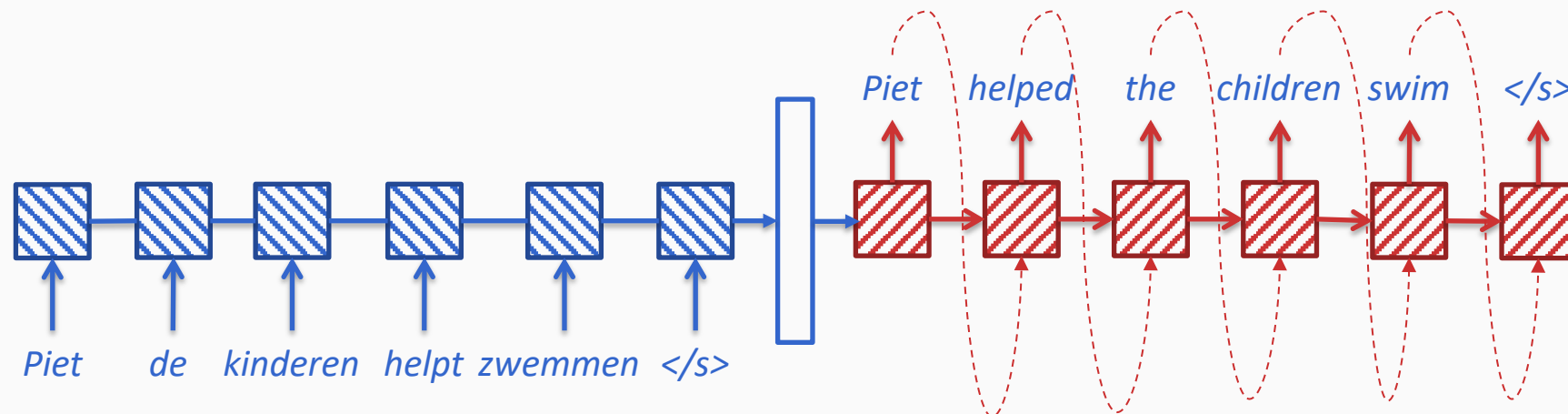
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The decoder produces probabilities over the output sequence words



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In practice: such a simple encoder-decoder network works for short sentences (10-15 words)

Needs other modeling refinements to improve beyond this

Adding attention to the decoder

[Bahdanau, 2014]

- Deciding on each output word does not depend on *all* input words
- Instead, if we can dynamically *attend* over the inputs for each output, then the decision of which output word to generate could be more targeted
- Let's build such a model from scratch

Step 1: The encoder

- Input sequence of words: x_1, x_2, \dots
 - Assume that we have special start and end tokens
- Bidirectional RNN (usually LSTM) encodes the sequence to produce a sequence of hidden states

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Concatenated states from the
left and right RNNs

Step 2: The decoder

- Suppose the output words are y_1, y_2, \dots
- For the i^{th} output word, suppose we summarize the input into a vector \mathbf{c}_i
 - We will look at what this vector is very soon
- The probability of i^{th} output word depends on
 - The previous word generated y_{i-1}
 - The hidden state of the decoder, say \mathbf{s}_{i-1}
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The previous word is represented by its embedding

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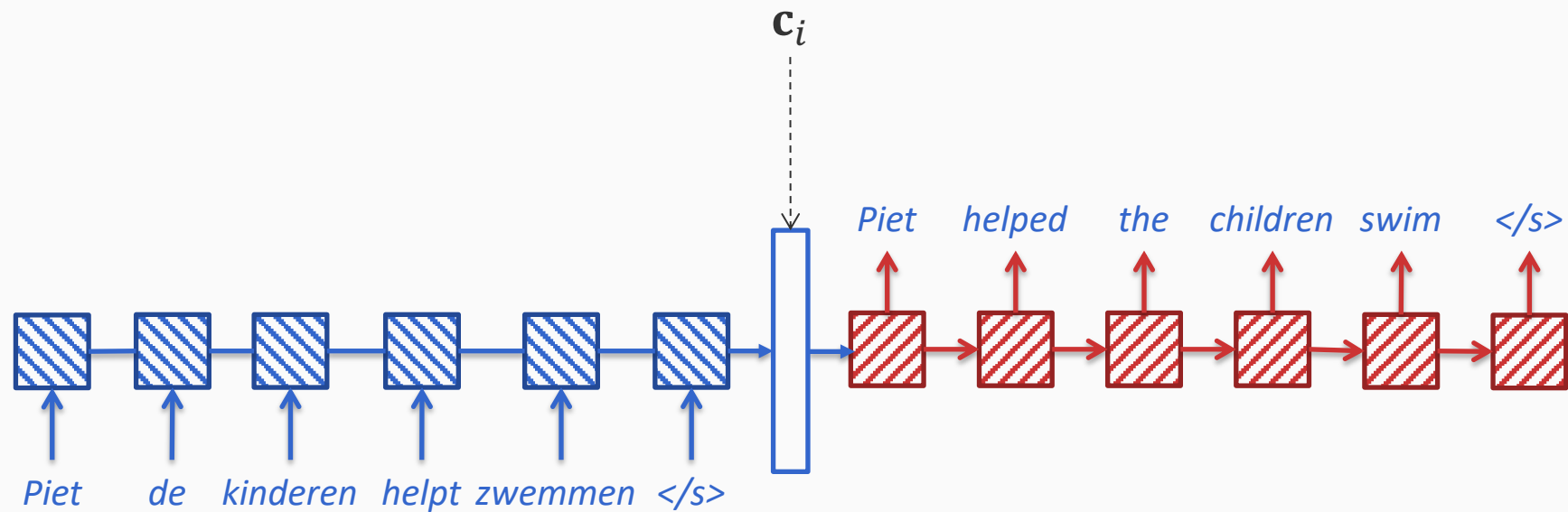
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Probability over all the target words

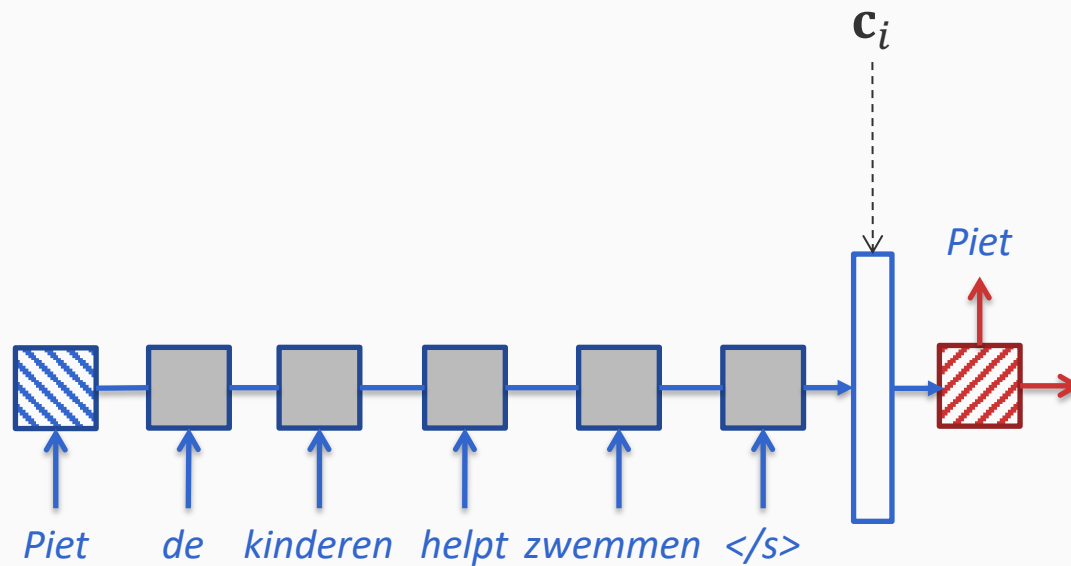
Summarizing inputs for generating outputs

At the i^{th} step, the vector \mathbf{c}_i should highlight information about the input words that is being translated



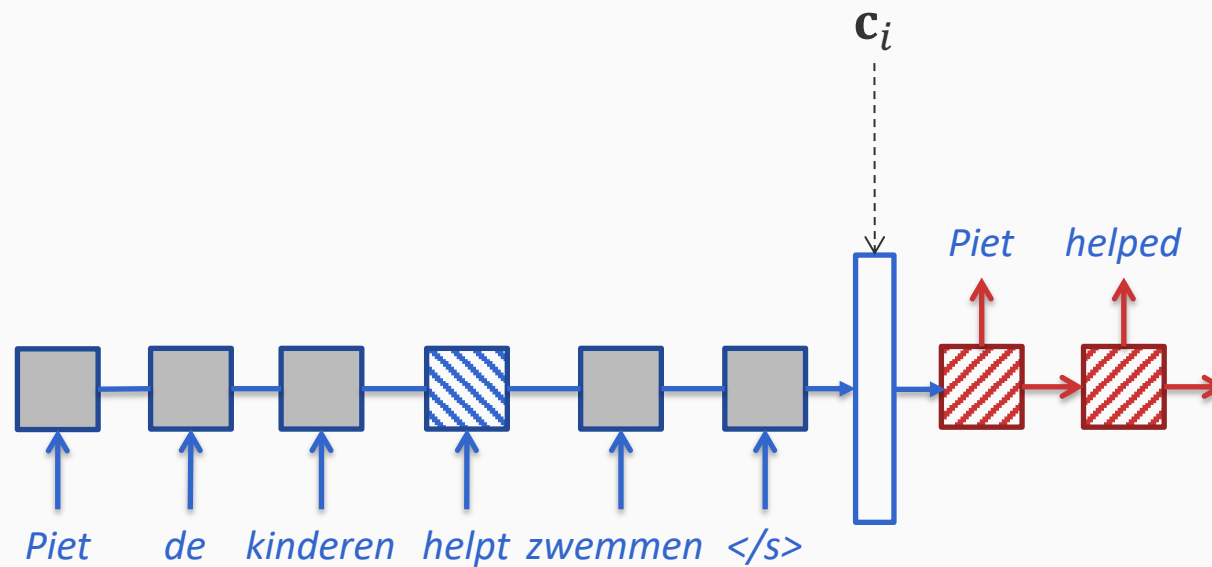
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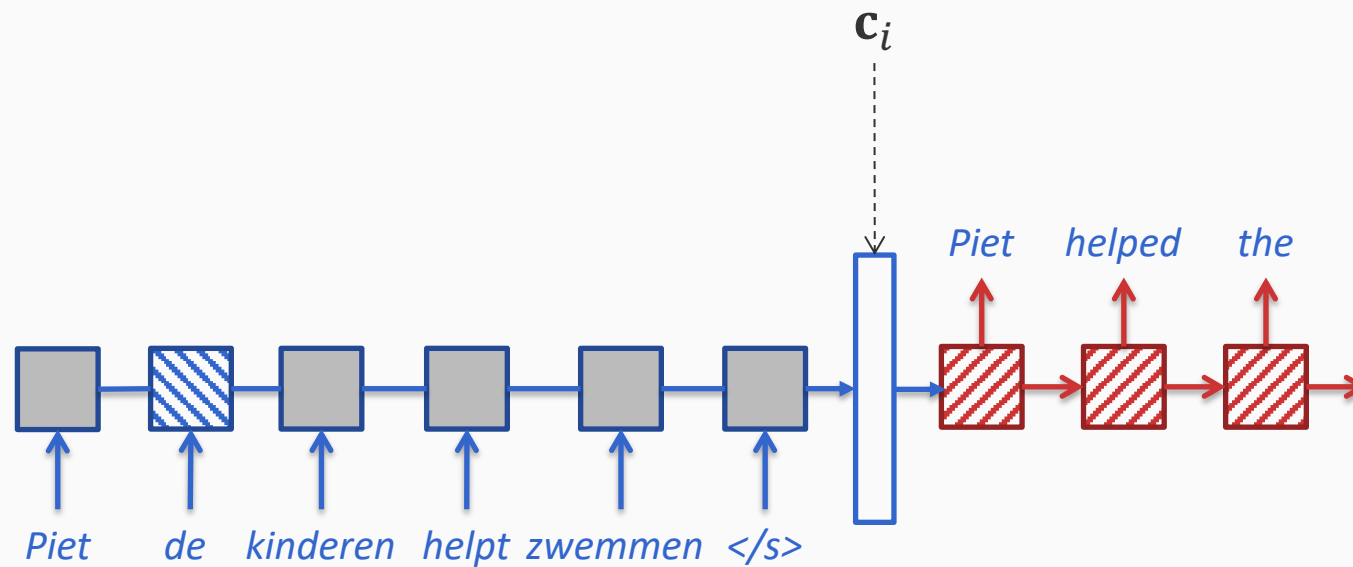
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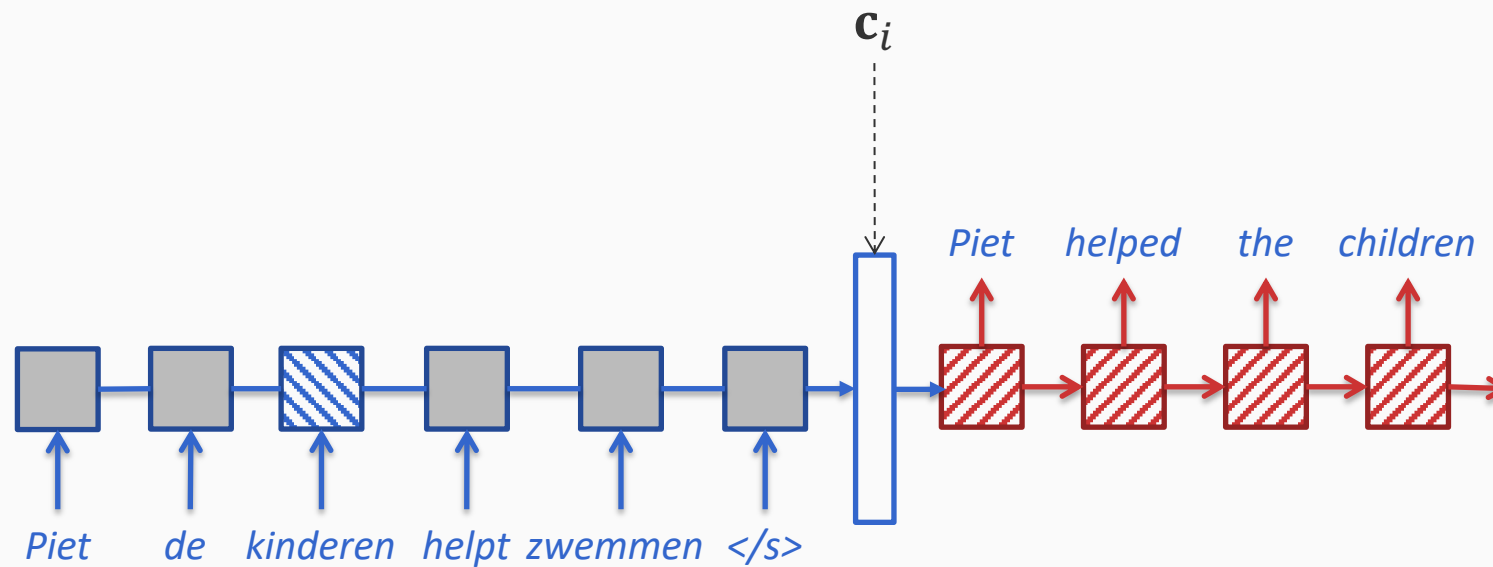
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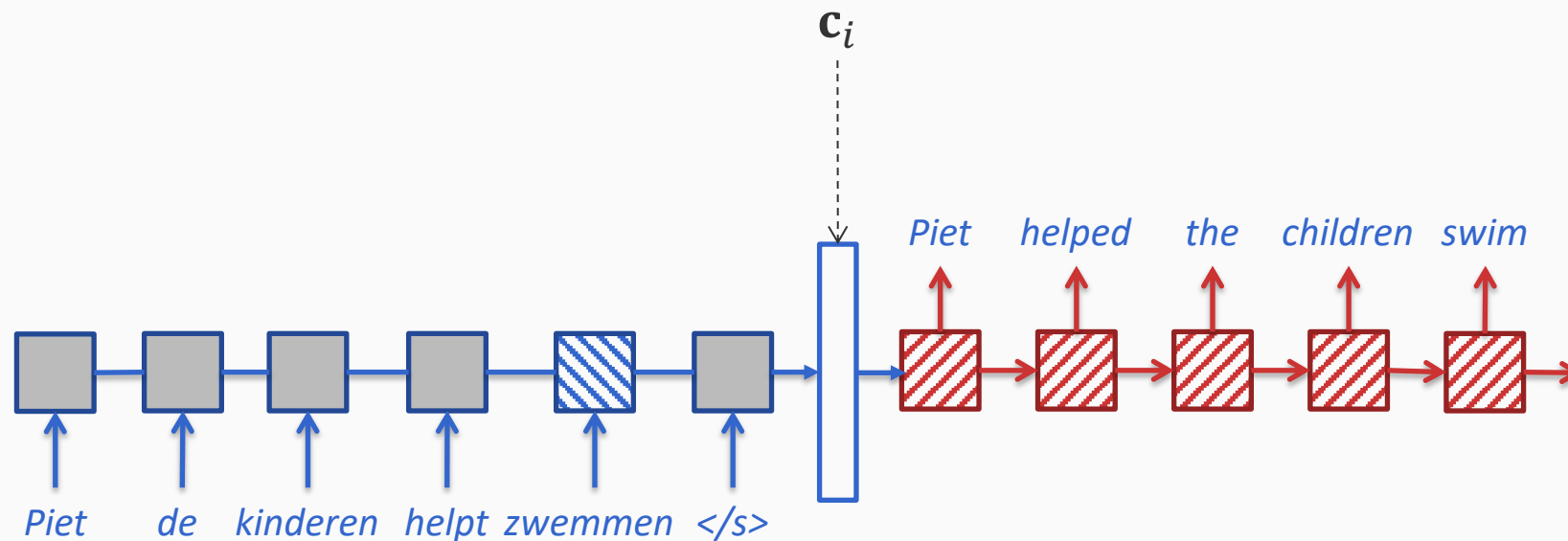
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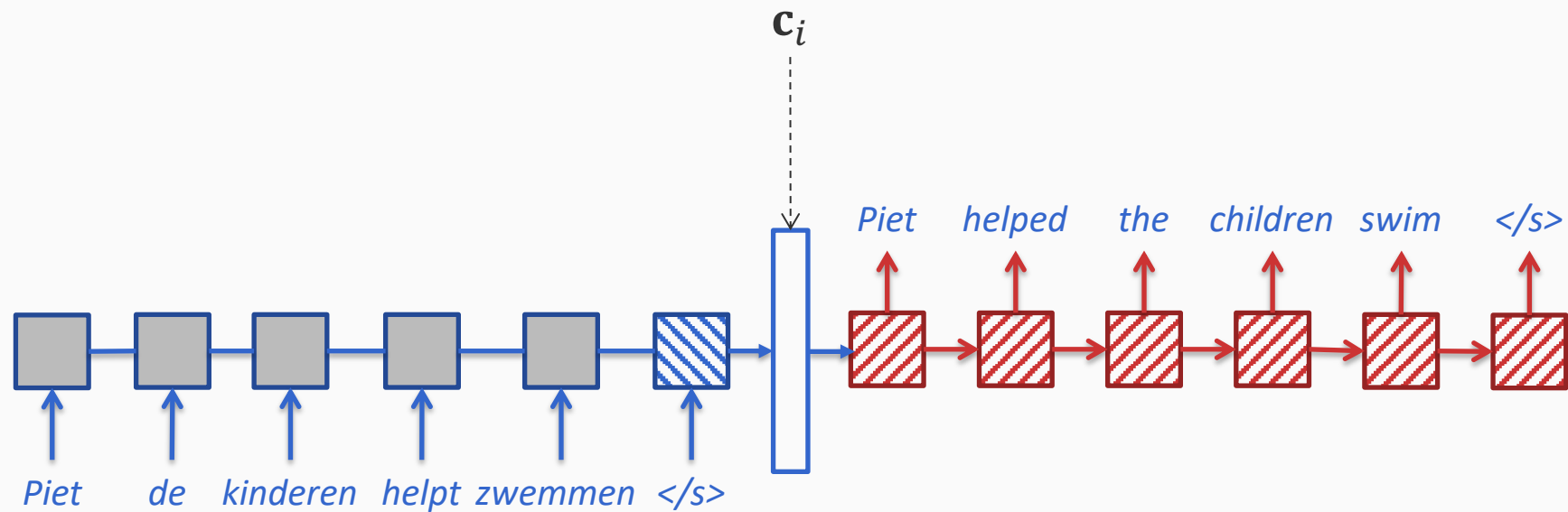
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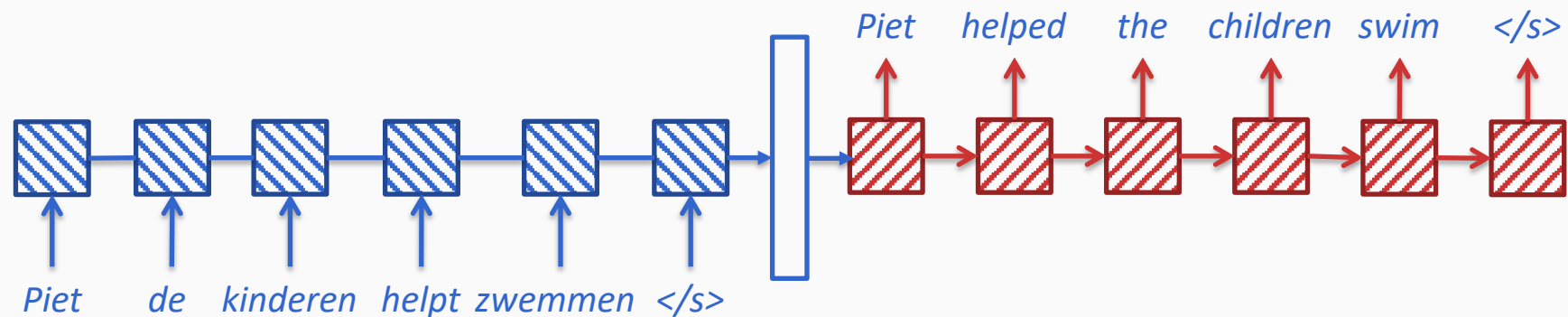
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At each step, this can be seen as a decision: *Which word is currently relevant?*

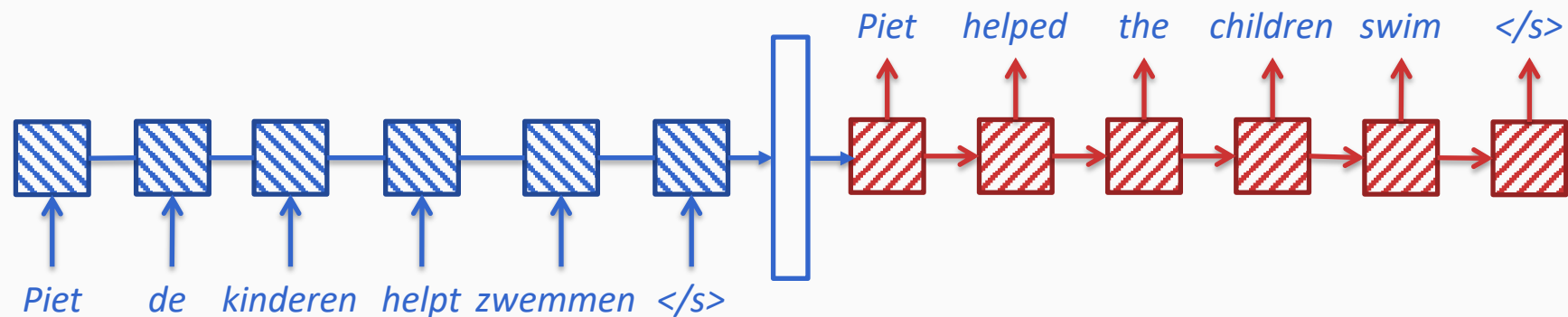


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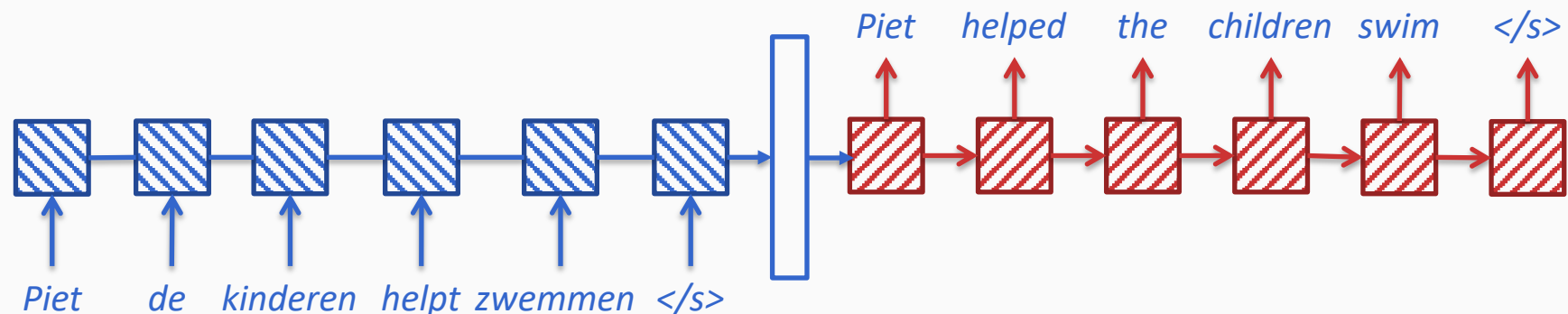
Instead of a hard decision, we can ask for a soft decision: a probability



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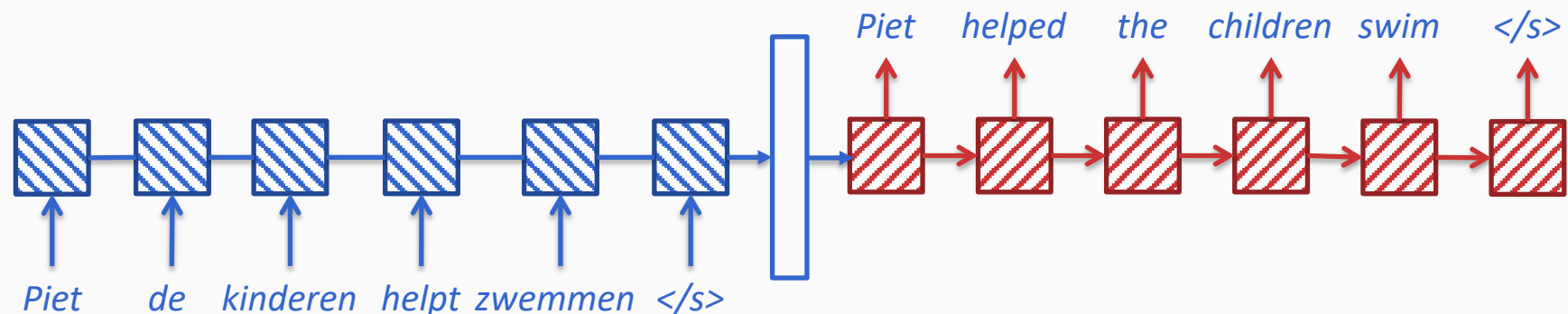
Let's see how we can construct the encoding using such a mechanism



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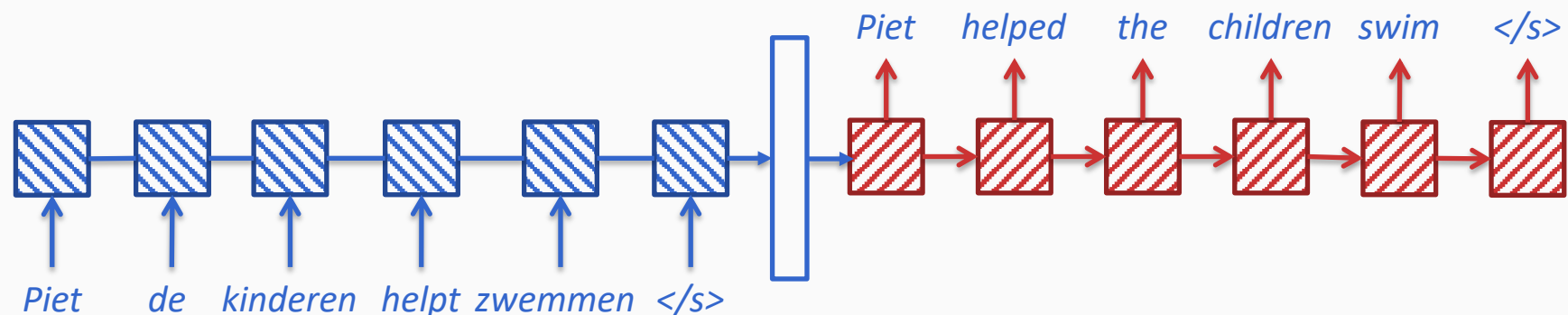


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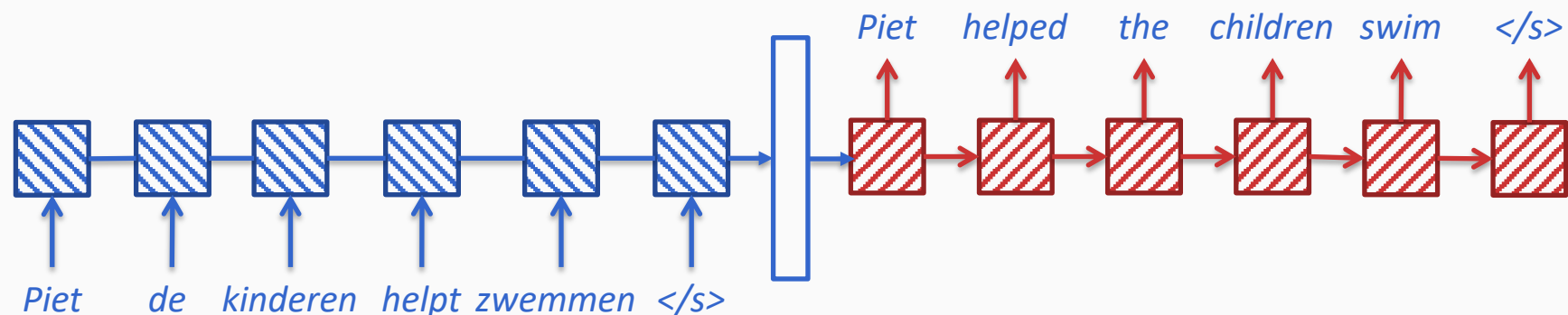
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A score that depends on the current state of the decoder and the word encodings

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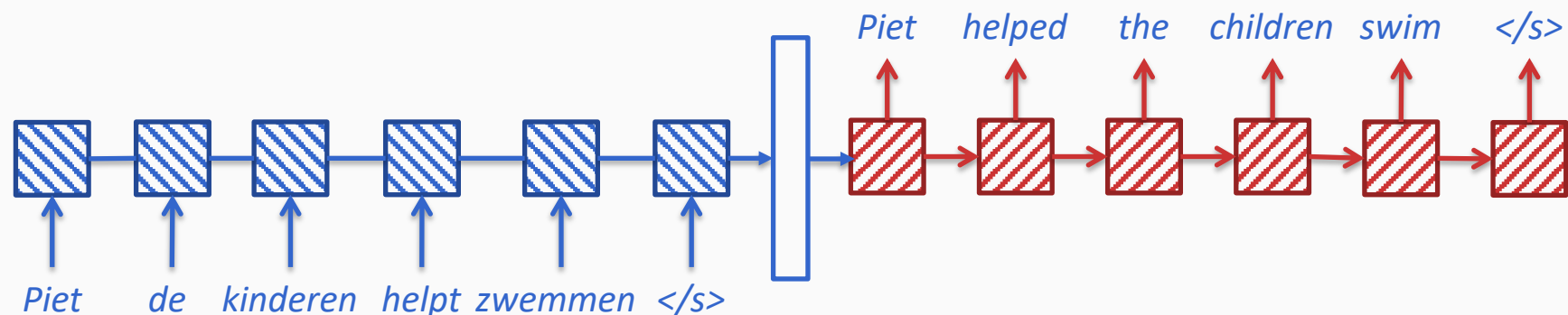
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Depends on the decoder



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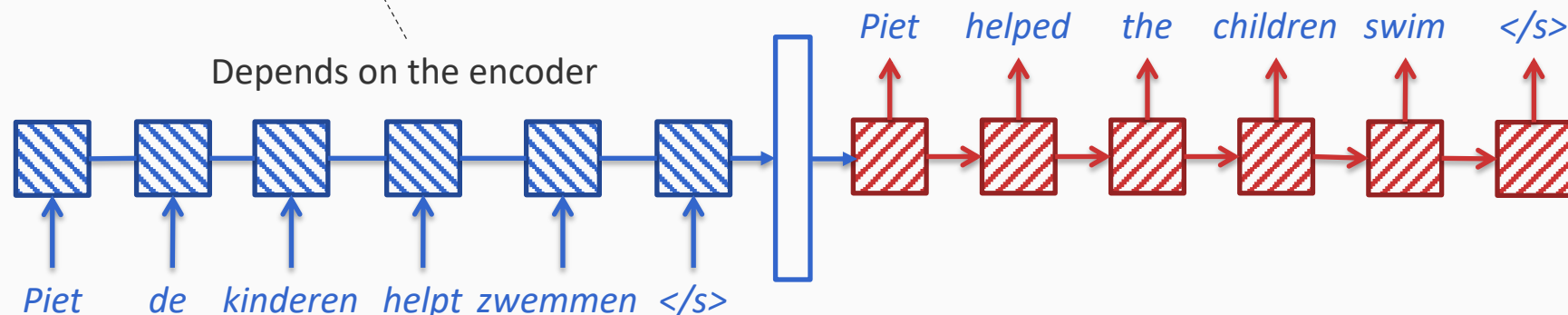
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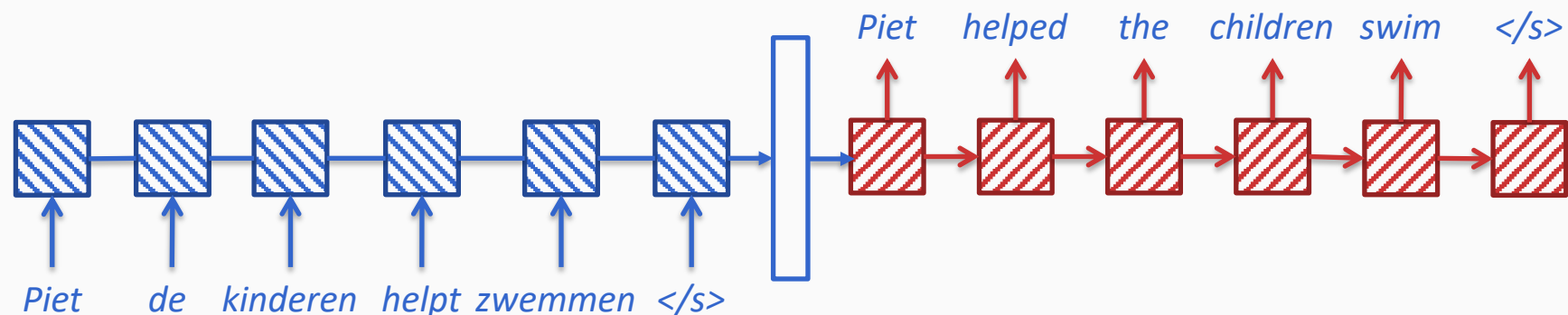
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Convert the score into a probability by taking softmax over the inputs

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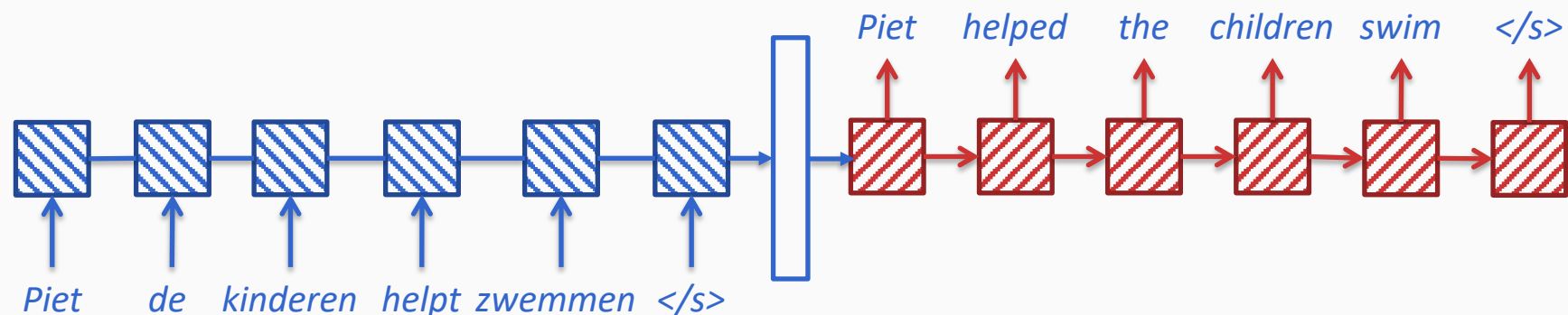
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Think of this as:

$P(\text{the } j^{th} \text{ input is relevant} \mid i - 1 \text{ outputs have been generated})$



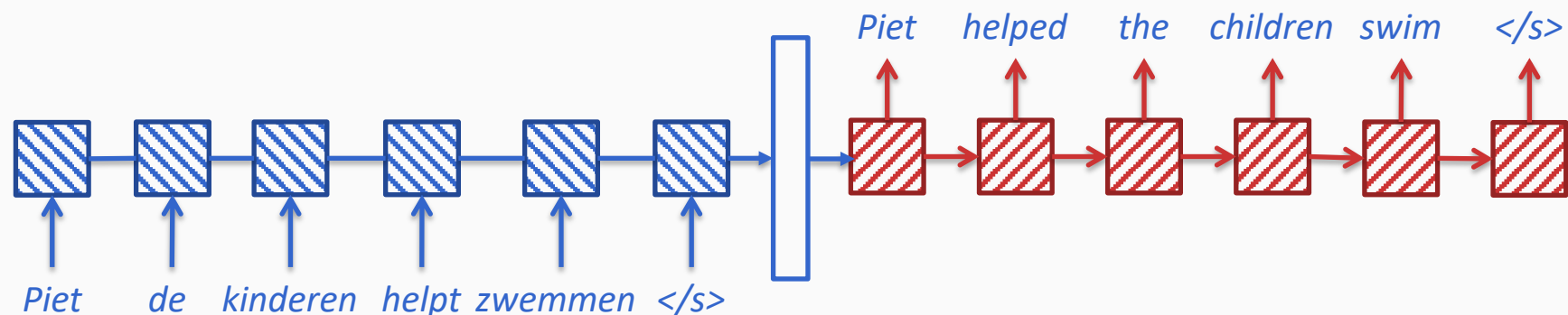
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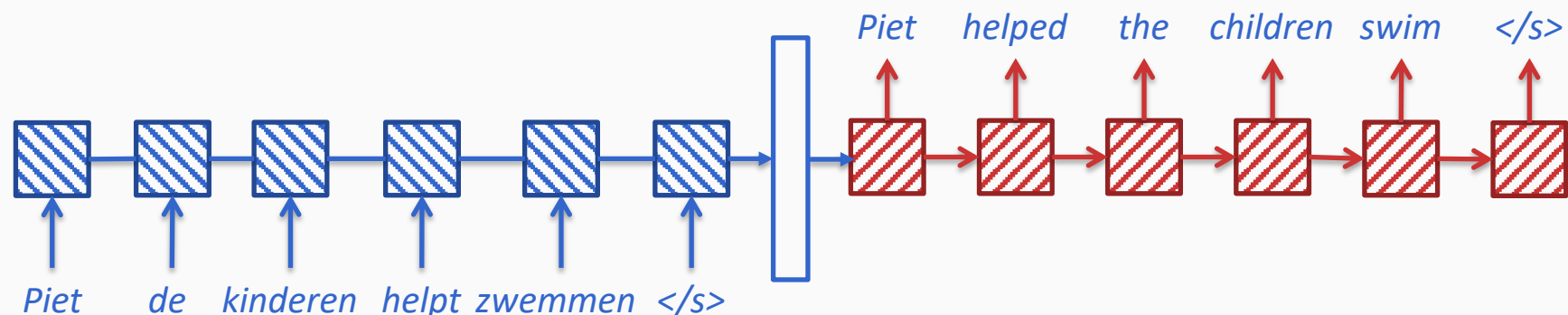
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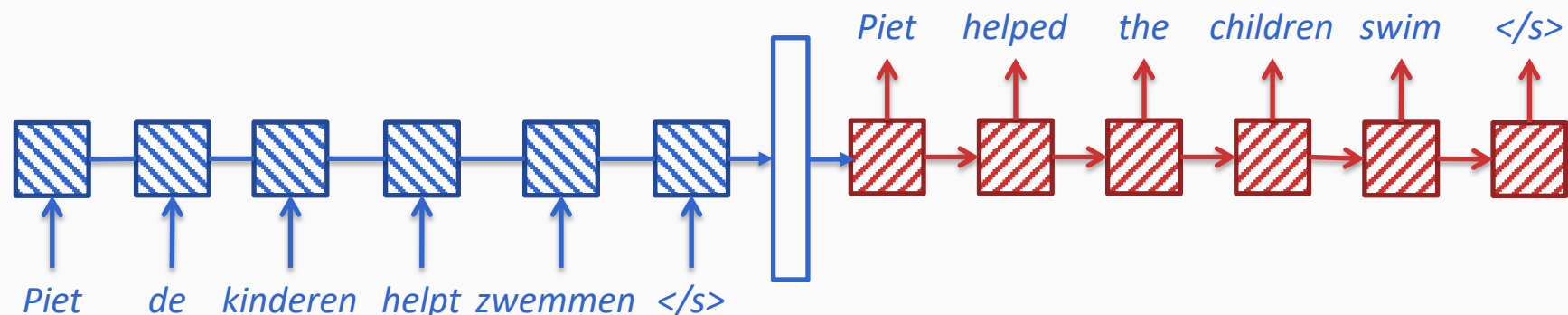
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- Given a prediction problem whose inputs consist of many sub-components
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Sometimes this is called the *source* sequence

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$$a(\mathbf{s}, \mathbf{h}_j) = W_a \mathbf{s} + W_I \mathbf{h}_j + b$$

2. Normalize with softmax to get attention

$$\text{Attention } a_j = \frac{\exp(a(\mathbf{s}, \mathbf{h}_j))}{\sum_k \exp(a(\mathbf{s}, \mathbf{h}_k))}$$

What we saw so far: Additive attention

1. Compute a score for each sub-component of the input

$$a(\mathbf{s}, \mathbf{h}_j) = W_a \mathbf{s} + W_I \mathbf{h}_j + b$$

2. Normalize with softmax to get attention

$$\text{Attention } a_j = \frac{\exp(a(\mathbf{s}, \mathbf{h}_j))}{\sum_k \exp(a(\mathbf{s}, \mathbf{h}_k))}$$

Why should the score be additive?
Maybe other functions are possible

Different scoring functions for attention

Name	Scoring function $a(\mathbf{s}, \mathbf{h}_j)$	Reference
Additive attention	$W_a \mathbf{s} + W_I \mathbf{h}_j + b$	Bahdanau et al 2015

We have already seen this

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We will see this in more detail when we visit Transformers

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In all cases, after the scoring function is applied, we have a softmax to produce the attention probability

Hard vs soft attention

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 - How relevant is each component in the context of a state s ?
 - Also called [soft attention](#)

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 - *Needs an expensive softmax*
 - **Can we avoid this?**

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- Attention is a probability over the input sub-components
 - How relevant is each component in the context of a state s ?
 - Also called **soft attention**
- What if there are *many* sub-components?
 - *Needs an expensive softmax*
 - **Can we avoid this?**
- **Hard attention**: Select one of the components – the argmax
 - Less computation
 - But not differentiable. How should this be trained?

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Also called *intra-attention*

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 - And we repeat this for each element
 - In our notation from before, \mathbf{s} is one of the \mathbf{h}_j 's
- Intuition: Compute attention over a sentence with respect to each word in the sentence
 - Captures interactions between the words of a sentence

Self-attention example

Cheng et al 2016

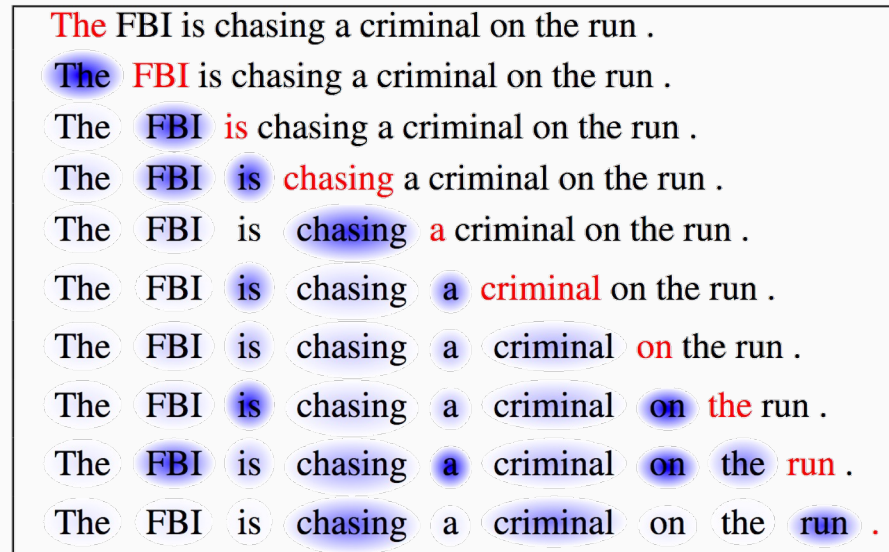


Figure 1: Illustration of our model while reading the sentence *The FBI is chasing a criminal on the run.* Color *red* represents the current word being fixated, *blue* represents memories. Shading indicates the degree of memory activation.

Why is self-attention interesting?

- Allows for contextual encoding of words
 - Weighted average of the attended word encodings
- Unlike a recurrent neural network, there is no sequential dependencies
 - Better parallelism for contextual encodings
- Forms the basis of the Transformer architecture which we will see next