

Recurrent Neural Networks



Overview

1. Modeling sequences
2. Recurrent neural networks: An abstraction
3. Usage patterns for RNNs
4. BiDirectional RNNs
5. A concrete example: The Elman RNN
6. The vanishing gradient problem
7. Long short-term memory units

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A simple RNN

- What we saw so far is just a template for a recurrent neural network
 - Did not specify what the functions inside it are
- Let's look at a simple instantiation, first introduced by Elman 1990

A simple RNN

At each step, an RNN:

- Computes the next cell state: $\mathbf{s}_t = \mathbf{R}(\mathbf{s}_{t-1}, \mathbf{x}_t)$
- Computes the output: $\mathbf{y}_t = \mathbf{O}(\mathbf{s}_t)$

Need to specify two functions:

1. How to generate the current state using the previous state and the current input?
2. How to generate the current output using the current state?

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Computing the value of a state

1. How to generate the current state using the previous state and the current input?

\mathbf{s}_{t-1}

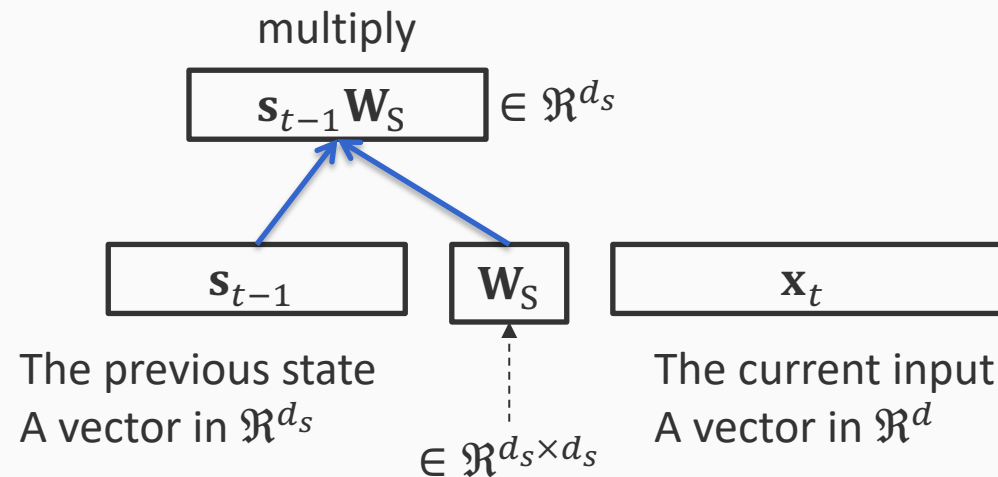
The previous state
A vector in \mathfrak{R}^{d_s}

\mathbf{x}_t

The current input
A vector in \mathfrak{R}^d

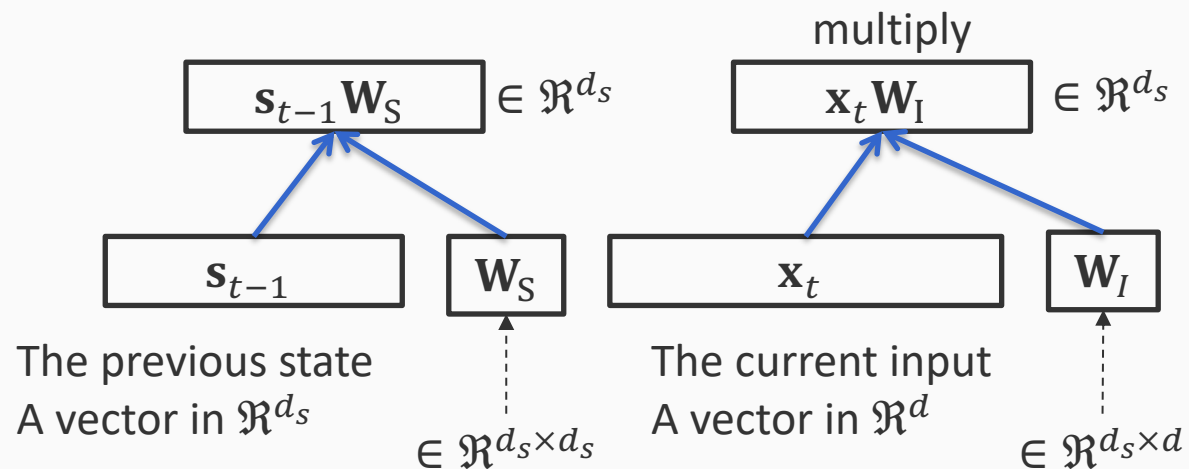
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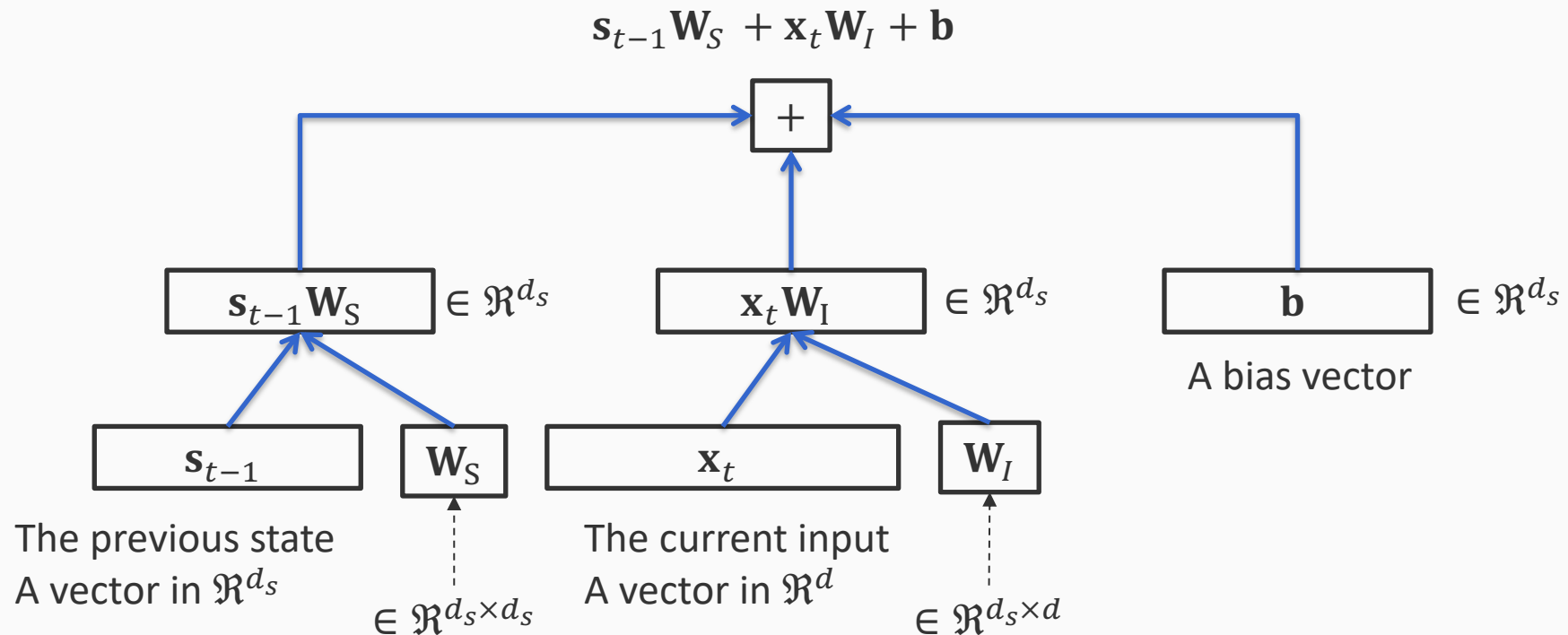
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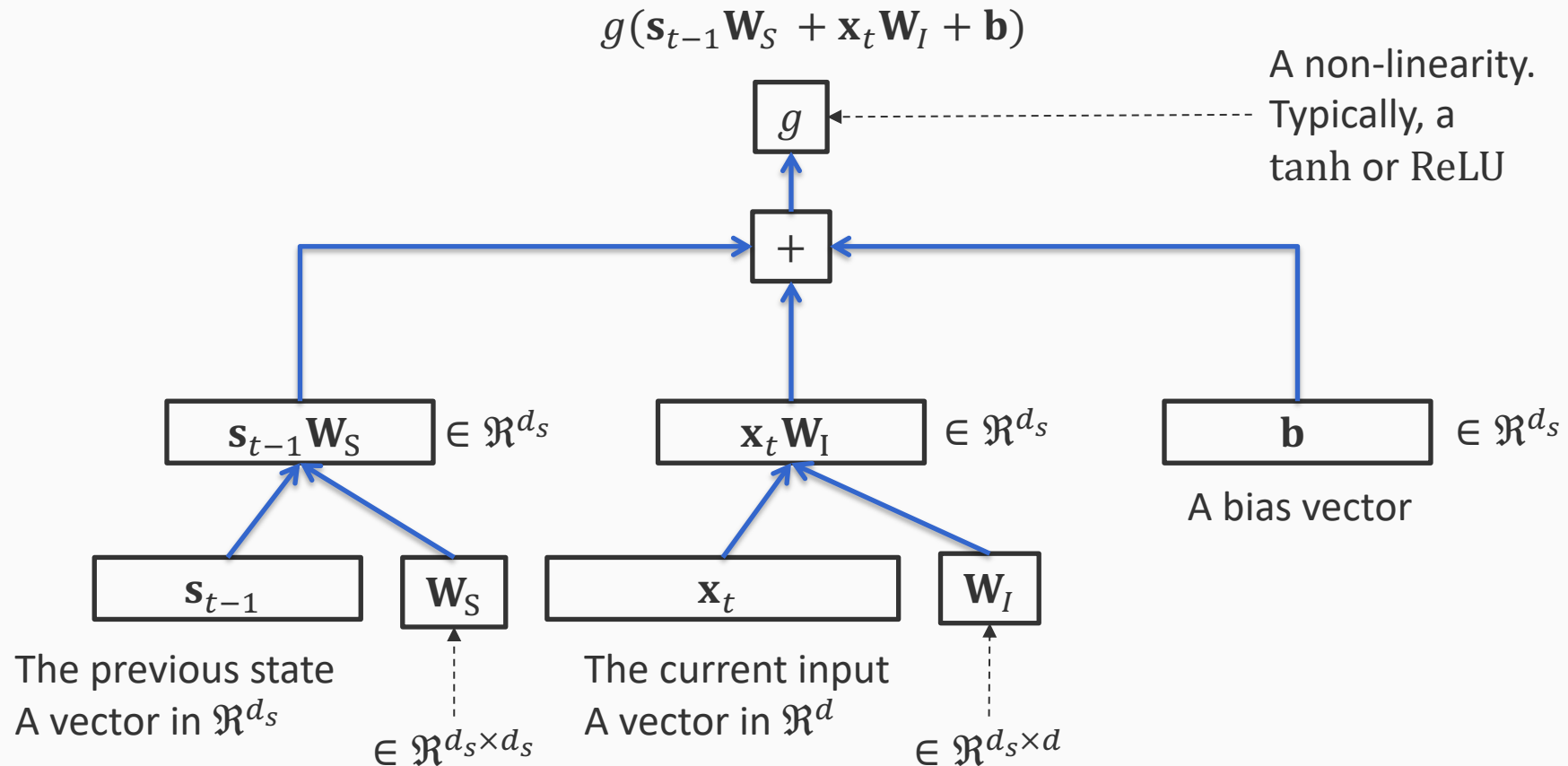
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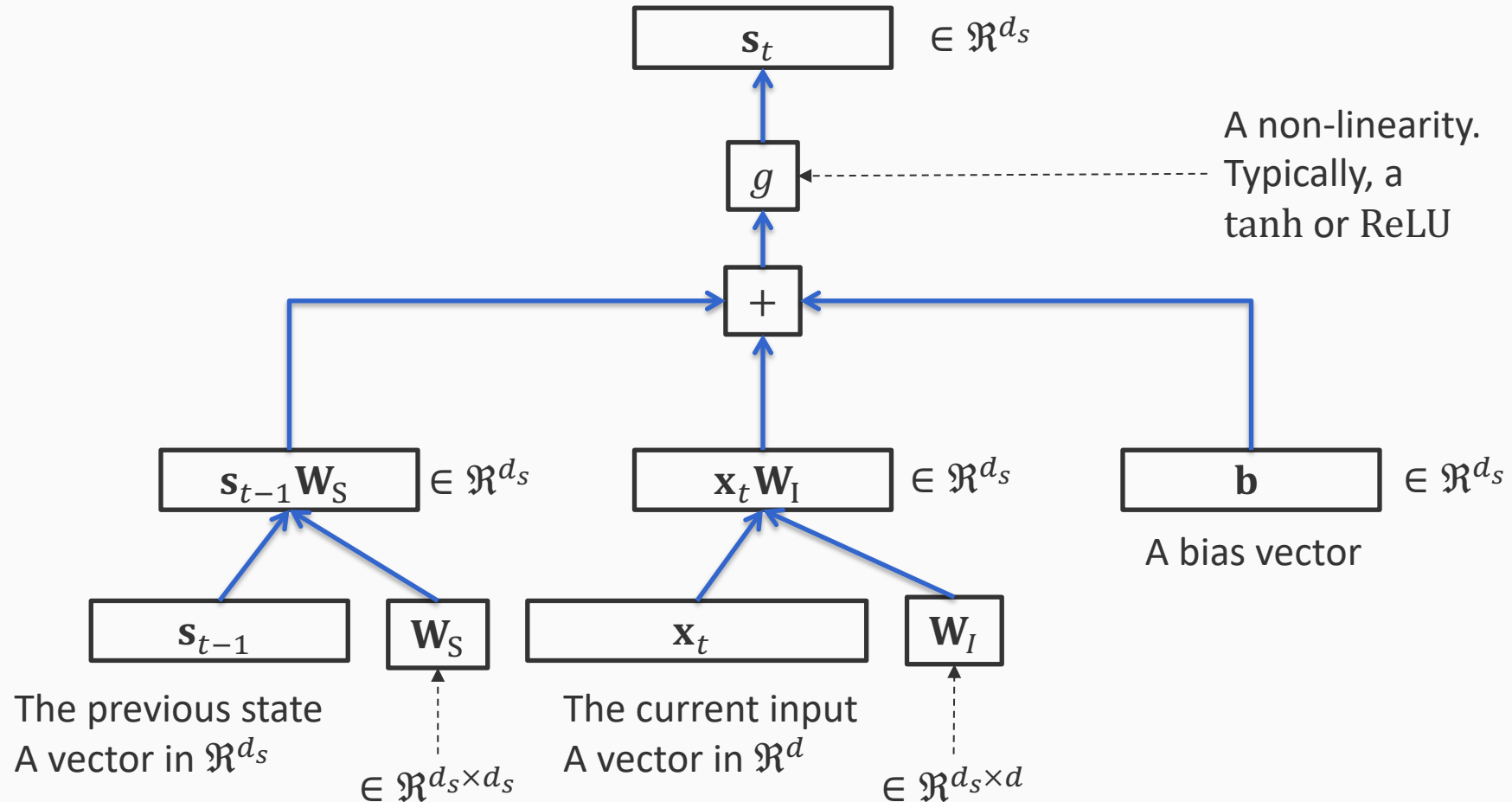
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Computing the value of a state

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$$\text{Next state } \mathbf{s}_t = g(\mathbf{s}_{t-1} \mathbf{W}_S + \mathbf{x}_t \mathbf{W}_I + \mathbf{b})$$



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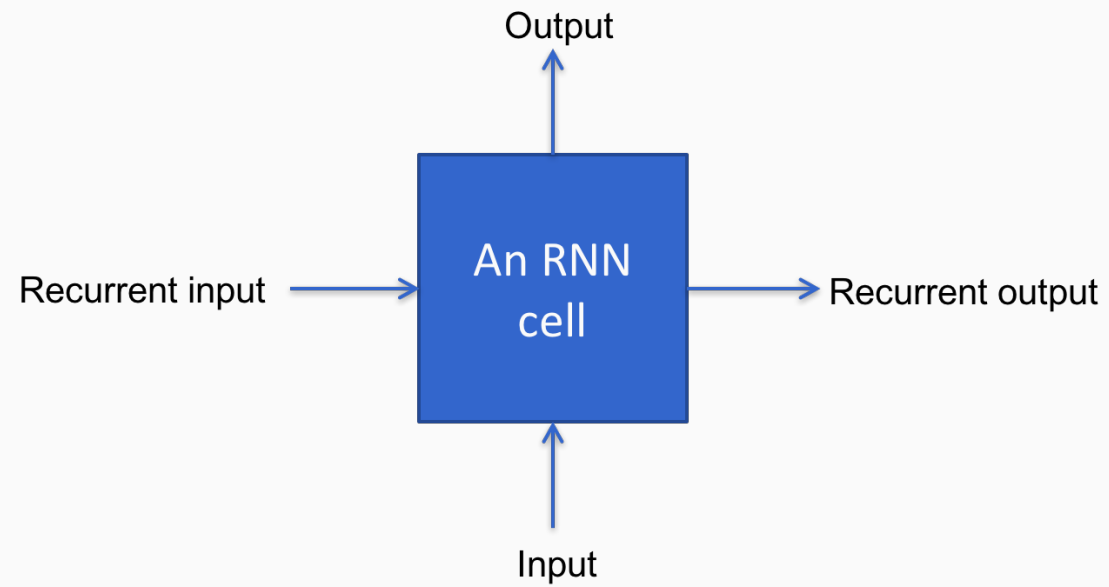
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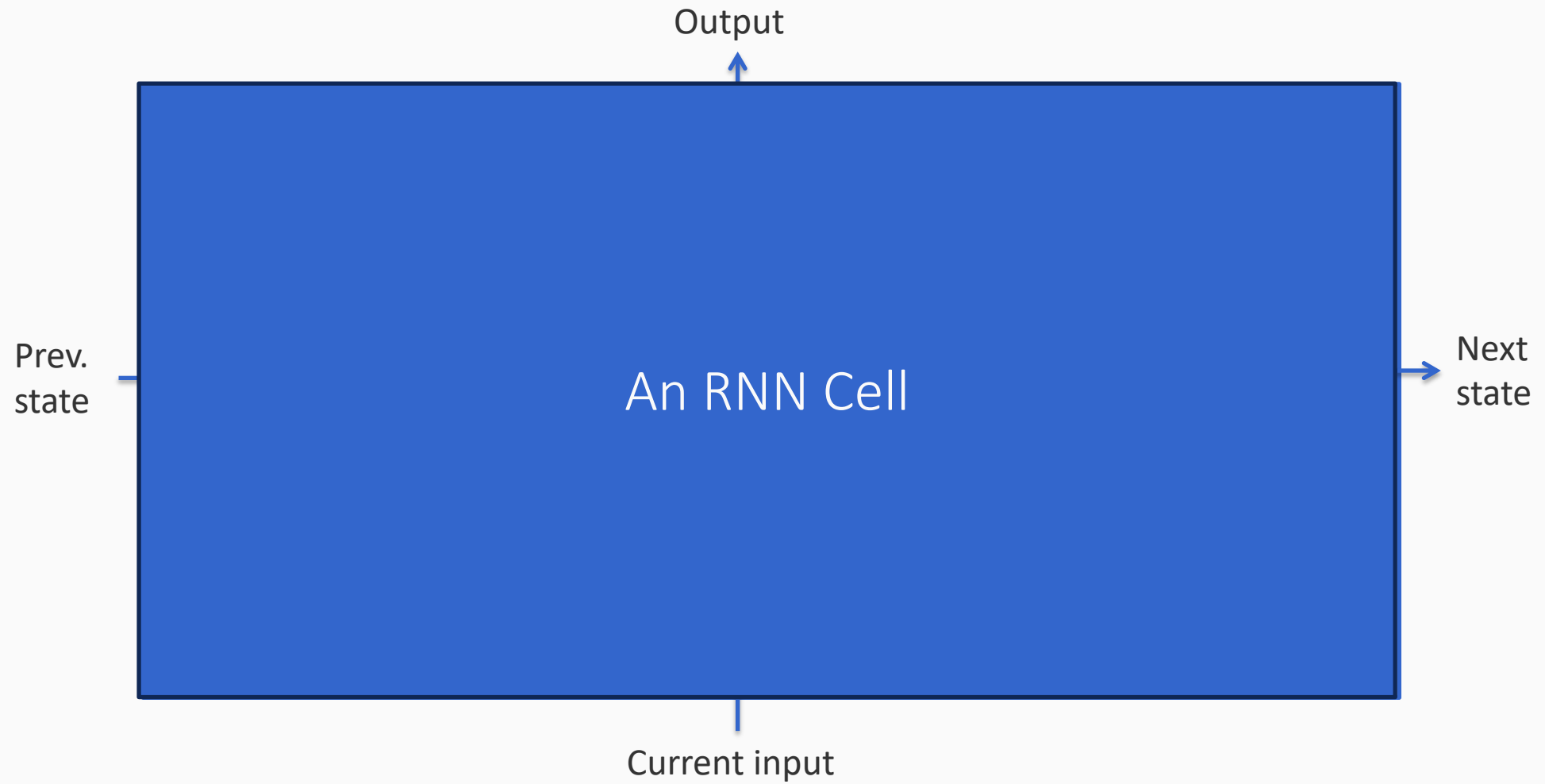
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The Elman RNN



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